් සියලු ම හිමිකම් ඇව්රිනි / மුழுப் பதிப்புரிமையுடையது / $All\ Rights\ Reserved)$

ලි ලංකා විභාග දෙපාර්තමේන්තුව ලි ලංකා විභාග දෙපාර්තමේන්තුව යි. ඉලු විභාග දෙපාර්තමේන්තුව ලි ලංකා විභාග දෙපාර්තමේන්තුව இலங்கைப் பரீட்சைத் திணைக்களம் இலங்கைப் பரீட்சைத் திணைக்களம் <mark>දිදුවේගේන් විභාග දෙපාර්තමේන්තුව ලි ලංකා විභාග දෙපාර්තමේන්තුව ලින්</mark>

> අධායන පොදු සහතික පතු (උසස් පෙළ) විභාගය, 2024 සබාබාට பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2024 General Certificate of Education (Adv. Level) Examination, 2024

ගණිතය I கணிதம் I Mathematics I 07 E I

ිපැය තුනයි ආණ්ඹු ගණ්ඩුන්මාග්ම **Three hours** අමතර කියවීම් කාලය - මිනිත්තු 10 යි மேலதிக வாசிப்பு நேரம் - 10 நிமிடங்கள் Additional Reading Time - 10 minutes

Use additional reading time to go through the question paper, select the questions you will answer and decide which of them you will prioritise.

| Index Number | | | |
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Instructions:

* This question paper consists of two parts; Part A (Questions 1-10) and Part B (Questions 11-17).

* Part A:

Answer all questions. Write your answers to each question in the space provided. You may use additional sheets if more space is needed.

* Part B:

Answer five questions only. Write your answers on the sheets provided.

* At the end of the time allotted, tie the answer scripts of the two parts together so that Part A is on top of Part B and hand them over to the supervisor.

* You are permitted to remove **only Part B** of the question paper from the Examination Hall.

For Examiners' Use only

| (07) Mathematics I | | | | |
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| | Part A |
| 1. | Let $A = \{x \in \mathbb{R}: 5 - 2x - 9 \ge 2\}$ and $B = \{x \in \mathbb{R}: 2x - 8 < 6\}$. Find $A \cup B$, $A \cap B$ and $B - A$. |
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| 2. | Let A, B and C be subsets of a universal set S. Show that $A - (A \cap B \cap C) = A - (B \cap C)$. |
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| 3. | Show that the compound proposition $(p \Rightarrow q) \lor (p \land q)$ is logically equivalent to the compound | nd |
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| | proposition $\sim p \vee q$. | |
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| 5. | Obtain a quadratic equation in x from the equation $\log_{10}(x+15) = 2 - \log_{10}x$. Hence, find the value of x satisfying the equation $\log_{10}(x+15) = 2 - \log_{10}x$. |
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| 6. | Find all real values of x that satisfy the inequality $\frac{x}{x-2} - \frac{1}{x} < 1$. |
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| 7. | The functions f and g are defined by $f(x) = 3x + 2$ and $g(x) = 0$. Find the value of x for which $f(g(x)) = 3$. | $\frac{6}{2x+3}.$ | | |
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| | Solve the equation $f^{-1}(g(x)) = 1$ for x . | | | |
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| 8. | Let $A \equiv (5, b)$ and $B \equiv (-1, 3b)$ be two points, where $b \in \mathbb{R}$. Also Find the values of b such that AB is perpendicular to OC , where $b \in \mathbb{R}$ is perpendicular to AB . | | | point of AB. |
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| 9. | A 13 m long ladder is resting on a horizontal ground, while leaning against a vertical wall (see the figure). The foot of the ladder is pulled away from the wall at a rate of 0.2 m s ⁻¹ . Find the rate at which the top of the ladder is sliding down the wall when the foot of the ladder is at a distance 12 m from the wall. | / |
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| 10. | Find the area of the region enclosed by the curves $y = x^2$ and $y = 4x - x^2$. | |
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| 10. | Find the area of the region enclosed by the curves $y=x^2$ and $y=4x-x^2$. | |

සියලු ම හිමිකම් ඇව්රිනි/(மුழුப் பதிப்புரிமையுடையது/All Rights Reserved)

ලී ලංකා විතාශ දෙපාර්තමේන්තුව ශී ලංකා විතාශ දෙපාර්තමේන්තුව කිරීම පිළිබුද්ධ සිටියින් සිටු විතාශ දෙපාර්තමේන්තුව ශී ලංකා විතාශ දෙපාර්තමේන්තුව ඉබත්කෙන්ට பුර්ධකළු නිශානයේනෙක්ව ඉබත්කෙන්ට பුර මෙල් සිටුන් සිටුන්වේ සිටුන්වේ නිශානයේනෙක්ව ඉබත්කෙන්ට පුර්ධකළු නිශානයෙනෙක් Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka ශී ලංකා විතාශ දෙපාර්තමේන්තුව ලී ලංකා විතාශ දෙපාරතමේන්තුව සිටුන්වේන්ට සිටුන්වේන්ට දියුනු විතාශ දෙපාරතමේන්තුව ලී ලංකා විතාශ දෙපාරතමේන්තුව ශී ලංකා විතාශ දෙපාරතමේන්තුව ශිලාන විතාශ දෙපාරතමේන්තුව නිශානයෙන්වේ පුරිධක්වේන දෙපාරතමේන්තුව ශිලානා විතාශ දෙපාරතමේන්තුව යි. ලංකා විතාශ දෙපාරතමේන්තුව ශිලානා විතාශ දෙපාරතමේන්තුව මේ ලංකා විතාශ දෙපාරතමේන්තුව ඉබත්කෙන්ට பුර්ධකළුන් නිශානයෙන්වා ඉහත්කෙන්ට පුරුන්වේන් සිටුන්වේන් සිටුන්වේන් සිටුන්වේන් සිටුන්වේන් සිටුන්වේන්ට සිටුන්වේන් සිටුන්වේන් සිටුන්වේන් සිටුන්වේන්ට සිටුන්වේන් සිටුන්වේන් සිටුන්වේන්ට සිටුන්වේන් සිටුන්වේන්ට සිටුන්වේන්ට සිටුන්වේන් සි

අධායන පොදු සහතික පතු (උසස් පෙළ) විභාගය, 2024 සබ්බාට பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2024 General Certificate of Education (Adv. Level) Examination, 2024

ගණිතය I සණෝதம் I Mathematics I

07 E I

Part B

- * Answer five questions only.
- 11. (a) While observing the G.C.E. (Ordinary Level) results for the subjects Mathematics, Science and English of 40 students in a G.C.E. (Advanced Level) class, the following information were revealed:
 - 20 students for Mathematics and 18 students for Science have obtained A grades.
 - 9 students for both Mathematics and Science, 8 students for both Science and English, and 5 students for both Mathematics and English have obtained A grades.
 - 10 students have obtained A grades only for two of the subjects among these subjects.
 - The number of students who have not obtained A grades for any of these three subjects is twice the number of students who have obtained A grades for all three subjects.

Find the number of students

- (i) who have obtained A grades for all three subjects,
- (ii) who have obtained A grade only for Mathematics,
- (iii) who have obtained A grade for English.
- (b) Using truth tables, show that
 - (i) $(p \land q) \lor r$ is logically equivalent to $(p \lor r) \land (q \lor r)$,
 - (ii) $(p \lor q) \land (\sim p \lor r) \Rightarrow q \lor r$ is a tautology.
- 12.(a) Using the Principle of Mathematical Induction, prove that

$$\sum_{r=1}^{n} \frac{1}{(2r-1)(2r+1)} = \frac{n}{(2n+1)} \text{ for all } n \in \mathbb{Z}^{+}.$$

(b) Let
$$f(r) = \frac{r}{(r+2)^2}$$
 for $r \in \mathbb{Z}^+$.

Find U_r such that $U_r = f(r) - f(r+1)$ for $r \in \mathbb{Z}^+$.

Show that
$$\sum_{r=1}^{n} U_r = \frac{1}{9} - \frac{(n+1)}{(n+3)^2}$$
 for $n \in \mathbb{Z}^+$.

Hence, show that $\sum_{r=1}^{\infty} U_r$ is convergent and find its sum.

Also, find
$$\sum_{r=15}^{\infty} U_r$$
.

13.(a) The roots of the equation $x^2 + px + q = 0$ are -3 and 5; where $p, q \in \mathbb{R}$.

Find the values of p and q.

Using these values of p and q, find the value of the constant $r \in \mathbb{R}$ for which the equation, $x^2 + px + q + r = 0$ has equal roots.

(b) Let $p(x) = 2x^3 + ax^2 + (a+4)x + 6$, where $a \in \mathbb{R}$. It is given that (x-2) is a factor of p(x). Find the value of a.

When a has this value, factorize p(x).

Also, solve the inequality p(x) > 0.

- **14.**(a) Find the first 3 terms in the expansion of $(1-x-x^2)^6$ in ascending powers of x. **Hence**, find the value of k such that the coefficient of x^2 in the expansion of $(k+x^2)(1-x-x^2)^6$ is 10.
 - (b) A person takes a loan of Rs. $500\,000$ from a bank that charges a monthly interest of 1%. He pays back the loan in equal monthly instalments of Rs. B over 5 years. Let Rs. A_n be the amount to be paid back after n months. Show that

$$A_2 = 500\,000 \, (1.01)^2 - B(1+1.01)$$
 and
 $A_3 = 500\,000 \, (1.01)^3 - B(1+1.01+1.01^2)$.

Write down a similar expression for A_n in terms of $n \leq 60$ and B.

Find the value of B.

15. Let the line l_1 be given by 4y = 3x + 1. The point $A \equiv (a, 4)$ lies on l_1 . Find the value of a. Suppose that the line l_2 is parallel to l_1 and passing through the point (4, -3). Find the equation of l_2 .

Let B be the point of intersection of l_2 and the y-axis, and C be the point on l_1 such that BC is perpendicular to l_1 . Find the coordinates of C.

Let D be the point such that ABCD is a parallelogram. Find the coordinates of D.

Also, find the area of ABCD.

16. (a) Evaluate
$$\lim_{x \to 1} \frac{(x^3 - 1)^2}{(\sqrt{x} - 1)(2x^2 - x - 1)}$$
.

(b) Differentiate each of the following with respect to x:

(i)
$$\sqrt{\ln(x^4e^x + 5x^2 + 3)}$$

(i)
$$\sqrt{\ln(x^4e^x + 5x^2 + 3)}$$
, (ii) $(2-3x^2)^7(x+2x^2)^5$, (iii) $\frac{3e^{x^2} + 2x^3}{3e^{x^2} - 2x^3}$

(iii)
$$\frac{3e^{x^2} + 2x^3}{3e^{x^2} - 2x^3}.$$

(c) A right circular hollow cylinder, open at one end, is constructed from a thin sheet of metal. The total outer surface area of the cylinder is 192π cm². The cylinder has a radius of r cm and a height of h cm.

Express h in terms of r, and show that the volume $V \text{ cm}^3$, of the cylinder is given by $V = \frac{1}{2}\pi \left(192r - r^3\right).$

Find the value of r such that V is maximum.

- 17.(a) Using partial fractions, find the value of $\int_{-1}^{2} \frac{1}{x^2(x+1)} dx$.
 - (b) Using integration by parts, find the value of $\int_{0}^{2} (12x^{3} + 4x) \ln x \, dx.$
 - (c) The following table gives the values of the function $f(x) = \ln(4 + x^3)$, correct to three decimal places, for values of x between 1 and 2 at intervals of length 0.25:

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|---------------------------------------|-------|-------------|-------|-------|-------|
| \boldsymbol{x} | 1 | 1.25 | 1.5 | 1.75 | 2.0 |
| f(x) | 1.609 | 1.784 | 1.998 | 2.236 | 2.485 |

Using **Simpson Rule**, find an approximate value for $\int_{-\infty}^{\infty} \ln(4+x^3) dx$.

Hence, find an approximate value for $\int_{1}^{2} \ln \left(\frac{1}{4+x^3} \right) dx.$

් සියලු ම හිමිකම් ඇවිරිණි / முழுப் பதிப்புநிமையுடையது / $All\ Rights\ Reserved]$

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අධායන පොදු සහතික පතු (උසස් පෙළ) විභාගය, 2024 கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2024 General Certificate of Education (Adv. Level) Examination, 2024

ගණිතය II கணிதம் II Mathematics II

07 E II

පැය තුනයි ආණ්ඹු மணித்தியாலம் **Three hours** අමතර කියවීම් කාලය - මිනීත්තු 10 යි மேலதிக வாசிப்பு நேரம் - 10 நிமிடங்கள் Additional Reading Time - 10 minutes

Use additional reading time to go through the question paper, select the questions you will answer and decide which of them you will prioritise.

Index Number

Instructions:

* This question paper consists of two parts;

Part A (Questions 1-10) and Part B (Questions 11-17).

Part A:

Answer **all** questions. Write your answers to each question in the space provided. You may use additional sheets if more space is needed.

Part B:

Answer five questions only. Write your answers on the sheets provided.

- * At the end of the time allotted, tie the answer scripts of the two parts together so that Part A is on top of Part B and hand them over to the supervisor.
- * You are permitted to remove only Part B of the question paper from the Examination Hall.
- * Statistical tables will be provided.

For Examiners' Use only

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| 8. | Let A and B be two events | on a sample | space S s | such that $P(A)$ | $= 0.4, P(A \cup$ | (B)' = 0.2 ar | nd |
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Bag ២ សិଡିකම් අවර්ණ /(மុழுப் பதிப்புநிமையுடையது /All Rights Reserved

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> අධායන පොදු සහතික පතු (උසස් පෙළ) විභාගය, கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2024 General Certificate of Education (Adv. Level) Examination, 2024

ගණිතය П கணிதம் II **Mathematics** II



Part B

- * Answer five questions only.
- 11. A manufacturer produces a certain product in two qualities: Grade I and Grade II. The same raw materials are used to produce both types. The amount of raw materials and labour hours needed to produce one unit in each quality and the profit per unit in each quality are shown in the table below:

| | Per unit values | | |
|--------------------|-----------------|------------------|--|
| | Grade I product | Grade II product | |
| Raw materials (kg) | 8 | 10 | |
| Labour hours | 6 | 5 | |
| Profit (Rs) | 140 | 100 | |

According to the market demand, at least 60 units from each quality must be produced per day. On each day, the manufacturer has 2 400 kg of raw material and 1 500 labour hours.

It is required to find the number of units to be produced per day from each quality to maximize the total profit.

- (i) Formulate this as a linear programming problem.
- (ii) Sketch the feasible region.
- (iii) Using the graphical method, find the optimum solution for this problem.
- (iv) During the production of 2 units of Grade II, if 1 unit of a by-product is obtained that gives a profit of Rs. 80 per unit, find the optimum solution under this new situation.

12. (a) Let
$$\mathbf{A} = \begin{pmatrix} 3 & a \\ -4 & 3 \end{pmatrix}$$
 and $\mathbf{B} = \begin{pmatrix} 4 & b \\ 0 & 2 \\ 1 & 1 \end{pmatrix}$, where $a, b \in \mathbb{R}$.

Find the values of a for which A^{-1} exists.

Now, let a = -2. Write down A^{-1} .

Let $C = BA^{-1}$. Find C in terms of b.

Find the value of b such that $\mathbf{C}^{\mathsf{T}}\mathbf{B} = \begin{pmatrix} 39 & 15 \\ 25 & 12 \end{pmatrix}$.

(b) Let $a, b \in \mathbb{R}$. Write down the system of linear equations

$$ax - y = 2$$

$$4x - 2y = b$$

in the form $\mathbf{AX} = \mathbf{B}$, where $\mathbf{X} = \begin{pmatrix} x \\ y \end{pmatrix}$, and \mathbf{A} and \mathbf{B} are matrices to be determined.

Show that the above system of equations has

- (i) a unique solution, when $a \neq 2$,
- (ii) infinitely many solutions, when a = 2 and b = 4,
- (iii) no solutions, when a = 2 and $b \neq 4$.
- 13.(a) An unbiased die with faces marked 1, 1, 2, 3, 4, 4 is rolled and an unbiased spinner with six separated regions numbered 1, 2, 3, 2, 2, 1 is spun.

The number on the top face of the die and the number on the region pointed by the arrow of the spinner are recorded.

Let A be the event that both recorded numbers are the same and B be the event that the sum of the two recorded numbers is even.

Find P(A'), $P(A' \cap B)$ and $P(A' \cup B)$.

(b) Numbers consisting of 5 digits are made by selecting digits from the seven digits from 1 to 7 without repeating any digit.

Find

- (i) the total number of different numbers that can be made,
- (ii) the number of different numbers that can be made starting with 3, and having 6 and 7 adjacent to each other.
- (c) A mathematics society consists of 9 senior members and 6 junior members. A research team of 5 people is to be formed to work on a new project.

Find the number of different ways in which the research team can be made

- (i) out of all members,
- (ii) such that the team has at least 3 senior members.
- 14. The probability that a school bus arrives on time on a Monday is 0.7. If the bus arrives on time on a particular day, the probability that it will be on time on the following day is 0.8. If the bus is late on a particular day, the probability that it will be late on the following day is 0.4.

Find the probability that the bus arrives on time on a Wednesday.

Also, find the probability that, from Monday to Wednesday of a week, the bus will be

- (a) late at least on one day,
- (b) late exactly on two days,
- (c) late exactly on two days, given that it was late at least on one day.

15. The actual weight of cashews in packets labelled as 50 g of a certain cashew distributor follows a normal distribution with a mean of 48 g and a standard deviation of 4 g. A packet of cashews is randomly selected. Let A be the event that the actual weight of cashews in the chosen packet is less than the labelled weight. Let B be the event that the difference between the actual weight of cashews in the chosen packet and the labelled weight is at most 2 g.

Find,

- (i) P(A),
- (ii) P(B),
- (iii) $P(A \cap B')$,
- (iv) P(A|B),

and

- (v) $P(A \cup B)$.
- 16. The following table summarises the distances travelled by a taxi driver during a certain period of time:

| Distance (km) | No. of days |
|---------------|-------------|
| 10 – 20 | 9 |
| 20 – 30 | 13 |
| 30 – 40 | a |
| 40 - 50 | 16 |
| 50 – 60 | 15 |
| 60 – 70 | 5 |

- (i) If the cumulative frequency corresponding to the 4th class interval is 60, find the value of a.
- (ii) Using the transformation $y_i = \frac{x_i 35}{10}$, or otherwise estimate
 - (a) total distance travelled, during this period of time,
 - (b) mean of the distance travelled per day,
 - (c) median of the distances travelled during this period of time.
- (iii) Based on the values of the mean and the median, what can be concluded about the shape of the distribution of the data?
- (iv) Sketch the cumulative frequency curve.
- (v) Using the curve sketched in part (iv), or otherwise, estimate
 - (a) the tenth percentile,
 - (b) the first quartile,
 - (c) the inter-quartile range

for the given data.

17. The duration of activities of a project and the flow of activities are given in the following table:

| Activity | Preceding Activity/ Activities | Duration (in months) |
|----------|--------------------------------|----------------------|
| A | | 3 |
| В | - | 4 |
| С | A, B | 5 |
| D | A, C | 2 |
| Е | С | 3 |
| F | B, C | 4 |
| G | D, E | 5 |
| Н | E, F | 6 |
| I | G, H | 1 |

- (i) Construct the project network.
- (ii) Prepare an activity schedule that indicates earliest start time, earliest finish time, latest start time, latest finish time and the float for each activity.
- (iii) Find the total duration of the project.
- (iv) Write down the critical path of the project.
- (v) What are the activities that can be delayed without extending the total duration of the project?
- (vi) How is the project completion time affected by delaying the activity F by 2 months?

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