සියලු හිමිකම් ඇවිරිණි / All Rights reserved වයඹ පළාත් අධනපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධනපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයම පළාත් අධ්යාපත දෙපාර්යමේ මුතු අධ්යාපත් වශයේ times (in Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්ට Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්ට Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්ට Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත දෙපාර්යමේන්තුව Provincial Department of Education - NWF වශය පළාත් අධ්යාපත වේත් වශය ප්‍යාධි විශ්යාපත වේත් වශය ප්‍යාධි විශ්යාපත වේත් වශය ප්‍යාධි විශ්යාපත වේත් විශ්යාපත විශ්යාපත වේත් විශ්යාපත විශ්යාපත වේත් විශ්යාපත වේත් විශ්යාපත වේත් විශ්යාපත විශ්යාපත වේත් විශ්යාපත විශ්යාපත වෙත් විශ්යාපත විශ්යාපත විශ්යාපත විශ්යාපත විශ්යාපත වෙත් විශ්යාපත විශ්යාපත විශ්යාපත විශ්යාපත විශ්යාපත වෙත් විශ්යාපත විශ්යාපත වෙත් විශ්යාපත විශ් Son cent cally to the lalin eparthrent of Education son Nakel Department වයඹ පළාත් අධ්නාපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නාපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නාපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නාපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නාපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නාපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP Second Term Test - Grade 13 - 2020 Combined Mathematics I Three hours only Index No:.... Instructions: * This question paper consists of two parts. Part A (Question 1 - 10) and Part B (Question 11 - 17) Answer all questions. Write your answers to each question in the space provided, you may use additional sheets if more space is needed. * Part B Answer five questions only. Write your answers on the sheets provided. * At the end of the time allocated, tie the answers of the two parts together so that Part A is on top of part B before handing them over to the supervisor. * You are permitted to remove only Part B of the question paper from the Examination Hall. For Examiner's Use only (10) Combined Mathematics I Paper I Paper II Part Question No Marks Awarded Total 1 **Final Marks** 2 3 4 **Final Marks** 5 A In Numbers 6 7 In Words 8 9 10 Marking Examiner Total 11 Marks Checked by 1 12 13 Supervised by 14 B 15 16 17

Total

Paper 1 total

Percentage

Combined Maths 13 - I (Part A)

Part A

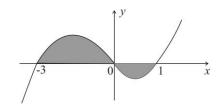
01.	Prove that $1+4+7++(3n-2)=\frac{n(3n-1)}{2}$ for all $n \in \mathbb{N}$, using the principle of mathematical
	induction.
0.2	
02.	Solve the inequality $ 3x-1 > x+3$, using graphs. Hence or otherwise , find the range of the values
	of x which satisfies the inequality $ 3x+5 > x+5$.

	Evaluate. $\lim_{x \to \frac{\pi}{4}} \frac{4\sqrt{2 - (\cos x + \sin x)}}{1 - \sin 2x}$
04 .	Write the r^{rh} term, Ur of the series $\frac{1}{2!}$, $\frac{2}{3!}$, $\frac{3}{4!}$, $\frac{4}{5!}$
04 .	Write the r^{th} term, Ur of the series $\frac{1}{2!}$, $\frac{2}{3!}$, $\frac{3}{4!}$, $\frac{4}{5!}$ If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04 .	<u> </u>
04 .	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04 .	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04 .	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.
04.	If $f(r) = \frac{1}{r!}$, write $f(r) - f(r+1)$ in terms of Ur and hence evaluate $\sum_{r=1}^{n} Ur$.

05. Find the equation of the normal drawn to the curve given by the parametric equations $x = (t+1)^2 t, \quad y = \frac{1}{2}t^3 + 3; t \ge -1 \text{ at the point where } t = 2.$

06. The figure shows a rough sketch of the graph

The figure shows a rough sketch of the graph y = x(x-1)(x+3). Fid the area of the finite region bounded by the curve and the x - axis.



.....

07.	Find the coordinates of the point on the parabola $y^2 = 8x$ which is at a minimum distance from
	the circle $x^2 + (y+6)^2 = 1$.
20	
08.	The equation of the perpendicular bisector of the sides AB and AC of a triangle ABC are
	x-y+5=0 and $x+2y=0$ respectively. If the point A is $(1,-2)$, then find the equation of the
	line BC.

09.	Find the equation of the circles which touches the axis of x and passes through the points $(1, -2)$ and $(3, -4)$.
10.	Find the solutions of the equation $\sin 6x + \cos 4x + 2 = 0$ within the range $0 \le x \le 2\pi$.

Combined Maths 13 - I (Part B)

Answer only 05 questions.

- 11. *a.* i. If the difference between the roots of the quadratic equation $x^2 3 + k(2x + 3) = 0$ is 2, find the value of k.
 - *ii.* If c is a real value in the quadratic equation $\frac{1}{x+1} + \frac{1}{x-1} = \frac{1}{c}$, show that the roots of this equation is real and distinct. Here $x \neq \pm 1$ and $c \neq 0$.
 - b. The polynomial $x^5 3x^4 + 2x^3 2x^2 + 3x + 1$ is denoted by f(x).
 - i. Show that neither (x+1) nor (x-1) is a factor of f(x).
 - ii. By substituting x=1 and x=-1 in the identity $f(x) \equiv (x^2-1)q(x) + ax + b$, where q(x) is a polynomial and a and b are constants, or otherwise, find the remainder when f(x) is divided by (x^2-1) .
 - iii. Show that the remainder when f(x) is divided by $(x^2 + 1)$ is 2x.
 - iv. Find all the real roots of the equation f(x) = 2x.
- 12. a. If the p^{th} and q^{th} terms of a geometric progression are q and p respectively, then show that its $(p+q)^{th}$ term is $\left(\frac{q^p}{p^q}\right)^{\frac{1}{p-q}}$.
 - b. Prove that $1 + n^2 + n^4 \equiv (1 + n^2)^2 n^2$.

Write the r^{th} term Ur of the series $\frac{1}{1+1^2+1^4} + \frac{2}{1+2^2+2^4} + \frac{3}{1+3^2+3^4} + \dots$

Using above identity or otherwise, find a function f(r) so that $\frac{1}{2}\{f(r)-f(r+1)\}=Ur$ and hence show that $\sum_{r=1}^{n} Ur = \frac{n(n+1)}{2(n^2+n+1)}$.

13. a. Prove that,

$$\cos\alpha + \cos(\alpha + \beta) + \cos(\alpha + 2\beta) + \dots + \cos[\alpha + (n-1)\beta] = \frac{\cos\left[\alpha + \left(\frac{n-1}{2}\right)\beta\right] \sin\left(\frac{n\beta}{2}\right)}{\sin\left(\frac{\beta}{2}\right)}$$

for all $n \in N$, using the principle of mathematical induction.

- b. In how many ways can the all the letters of the word PERMUTATIONS be arranged to form different words. Among those formations find the number of words
 - i. starts with P and ends with S.
 - ii. where the vowels are all together
 - iii. where four letters are in between P and S.
- c. A committee of 7 members has to be formed from 9 boys and 4 girls. In how many ways can this be done when the committee consists of
 - i. exactly 3 girls
 - ii. at least 3 girls
 - iii. at most 3 girls.

14. a. Let
$$f(x) = \frac{16(x+1)}{(x-1)^2(3x+1)}$$
 for $x \ne 1$ and $x \ne -\frac{1}{3}$.

Show that the derivative of f(x), f'(x) is given by $f'(x) = \frac{-32x(3x+5)}{(x-1)^3(3x+1)^2}$.

Write the equations of the asymptotes of y = f(x).

Find the coordinates of the intersection points of the horizontal asymptote and the curve of y = f(x).

Draw a rough sketch of the graph of y = f(x) representing the turning points and asymptotes.

- b. i. A tent is going to be formed as a right square pyramid. The distance to the each mid-point of each side of the square base from the top vertex is $3\sqrt{6} \ m$. If the area of the square base is A then, show that its volume V " is given by $V = \frac{A}{6}\sqrt{216 A}$.
 - *ii.* Find the value of A such that V is the maximum and hence, find the height of tent and the length of a side of the base of the tent.
 - *iii.* If the same kind of cloth is used to make the base and faces of the tent, find the required amount of cloth to make the tent having a maximum space inside the tent.
- 15. a. Find the constants A and B such that $\frac{1}{(1-z)(1-2z)} = \frac{A}{1-z} + \frac{B}{1+2z}.$

Using the substitution $t = \sin x$, show that $\int \frac{\sin x}{\sin 4x} dx = \frac{1}{4} \int \frac{dt}{(1-t^2)(1-2t^2)}.$

Hence, show that $\int \frac{\sin x}{\sin 4x} dx = P \ln \left| \frac{1 + \sin x}{1 - \sin x} \right| + Q \ln \left| \frac{1 + \sqrt{2} \sin x}{1 - \sqrt{2} \sin x} \right| + C \quad ; \quad C \quad \text{is an arbitrary}$ constant and P, Q the constants to be determined.

b. If f(x) is a function which is possible to integrate within the closed range [a, b], prove that

$$\int_{a}^{b} f(x)dx = \int_{a}^{b} f(a+b-x)dx.$$

It is given that $I = \int_a^b \sqrt{\frac{x-a}{b-x}} dx$ and $J = \int_a^b \sqrt{\frac{b-x}{x-a}} dx$. Prove that I = J.

Hence, prove that $I = \frac{\pi}{2}(b-a)$.

c. By using integration by parts, find $\int e^{3x} \sin 4x dx$.

16. a. Find the perpendicular distance to the line ax + by + c = 0 from a point $P(x_1, y_1)$.

In a triangle ABC, A = (7,11) and the equation of the side BC is 3x - 4y - 2 = 0. The ordinate of the mid-point of the side BC is 1 and the area of the triangle ABC is 30 square units. Find the coordinates of B and C.

b. Show that the general equation of the circle which touches the x- axis is $x^2 + y^2 + 2gx + 2fy + g^2 = 0$; g and f are real constants.

A variant circle touching x - axis passes through the point A(-1,3). Show that the path of the other end of the diameter passes through A of the circle is given by $y = \frac{1}{12}(x+1)^2$.

- 17. a. Draw the rough sketches of the graphs of $y = 2|\cos 2x|$ and $y = 1 + \sin x$ on the same diagram within the range $0 \le x \le 2\pi$. Hence state the number of solutions of the equation $2|\cos 2x| = 1 + \sin x$ within the above range.
 - b. State and prove the **sine rule** for any triangle ABC in the usual notation.

If $\frac{\sin(A-B)}{\sin(A+B)} = \frac{a^2 - b^2}{a^2 + b^2}$; $(\hat{A} \neq \hat{B})$ in the usual notation, for any triangle ABC, show that the triangle is right-angled.

c. Find the values of x which satisfies the equation $\tan^{-1} x + \tan^{-1} 2x = \frac{2\pi}{3}$.

සියලු හිමිකම් ඇවිරිණි / All Rights reserved වයඹ පළාත් අධනපත දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධනපත දෙපාර්තමේන්තුව Provincial Department of Education - NWF Dan cert and present the state of the state වයඹ පළාත් අධ්නාපන දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නපන දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නපන දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නපන දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නපන දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නපන දෙපාර්තමේන්තුව Provincial Department of Education - NWP වයඹ පළාත් අධ්නපන දෙපාර්තමේන්තුව Provincial Department of Education - NWP Second Term Test - Grade 13 - 2020 Combined Mathematics II Three hours only Index No:..... Instructions: * This question paper consists of two parts. Part A (Question 1 - 10) and Part B (Question 11 - 17) Answer all questions. Write your answers to each question in the space provided, you may use additional sheets if more space is needed. Answer five questions only. Write your answers on the sheets provided. * At the end of the time allocated, tie the answers of the two parts together so that Part A is on top of part B before handing them over to the supervisor. * You are permitted to remove only Part B of the question paper from the Examination Hall. For Examiner's Use only Paper I (10) Combined Mathematics II Paper II Part **Question No** Marks Awarded Total Final Marks 2 3 4 Final Marks 5 A In Numbers 6 7 In Words 8 9 10 Marking Examiner Total 11 Marks Checked by 1 12 13 Supervised by 14 B 15 16 17

Total

Paper /1 total

Percentage

(Part A)

01)	A thin smooth tube AB which is bent as an arc of radius a is fixed in a vertical plane so that its open ends A vertical and B horizontal. A particle Q of mass m is placed on the lowest point B of the tube and another particle P of mass m is projected vertically downwards to the tube with an initial velocity of $\sqrt{2ga}$. Particle P moving along the tube collides and coalesces with the particle Q at B . Find the velocity of the composite particle when it leaves the tube. (Here g is the gravitational acceleration.)	A Q M B
02)	The motion of a particle projected under the gravity with a velocity u inclined at an is perpendicular to the initial direction of projection after the time t . Show that t = gravitation1 acceleration.)	-

03)	A smooth light pulley is fixed to a smooth plane inclined at an acute angle α to the horizontal as shown in the figure. Two particles of mass $2m$ and m are connected to the ends of a light inextensible string passing over a pulley and released gently. Show that the acceleration of each particle is $\frac{g \sin \alpha}{3}$ and the tension of the string is $\frac{4}{3}mg \sin \alpha$.
04)	A car of mass $M kg$ moves with a constant velocity of $v ms^{-1}$ along a level road against a resistance of $R N$ with a constant power of $H kw$. Show that the resistance on the car $R = \frac{H \times 10^3}{V} N$.
	Then, the car moves down along a road inclined at an angle α to the horizontal with a velocity of $\frac{v}{2}$ ms ⁻¹ and same power H kw against the same resistance R N . Show that the acceleration of the car is $\left\{\frac{H \times 10^3}{Mv} - g \sin \alpha\right\}$ ms ⁻² . (Here g is the gravitational acceleration.)

05)	In the usual notation the position vectors of the points A, B and C are $(2\underline{i} + 4\underline{j})$, $(4\underline{i} + 4\underline{j})$ and
	$(\lambda \underline{i} + \mu \underline{j})$ respectively. Here λ and μ are real constants. When 0 is the origin, $0ABC$
	respresents a trapezium. Here <i>OA</i> and <i>CB</i> are parallel and $CB = \frac{1}{2} OA$. Find the values of λ
	and μ . If $A\hat{O}C = \theta$, show that $\cos \theta = \frac{7}{\sqrt{65}}$.
06)	A particle P of mass m is freely suspended by means of a light inextensible string of length l fixed to a
	point O. A velocity of $\sqrt{3l\ g}$ is given to the particle in the direction perpendicular to OP (horizontal).
	When <i>OP</i> makes an acule angle $\cos^{-1}\left(\frac{3}{5}\right)$ with the downward vertical, find the velocity of the particle
	P. Show that the tension of string is $\frac{14 mg}{5}$. (Here g is the gravitation acceleration.)

07)	As shown in the figure a square shape portion which is symmetrical about OA and the diagonal equals to the radius is removed from a circular lamina of radius r . Show that the center of gravity of the remaining part lies on the axis of symmetry OA at a distance $\frac{(4\pi-3)}{2(2\pi-1)}r$ from O .	O r A
	One end of an elastic string of natural length l and modu and a particle P of mass m is attached to the other end. Inivertically down with a velocity of $\sqrt{2 lg}$. Using the lav distance that can be moved by the particle from O .	tially the particle P is placed at O and projected

09)	Given that $P(A \cup B) = \frac{9}{10}$, $P(A') = \frac{1}{3}$, $P(B) = \frac{1}{2}$. Find $(A \cap B)$ and $P(A' \cap B)$. Here A' is the complement of event A .
10)	A box contains n number of red identical balls and 4 blue identical balls. Two balls are drawn without any replacement. If the probability that both balls drawn out are being red is $\frac{1}{3}$, find the value of n .

Combined Maths 13 - II (Part B)

11) (a) A space shuttle starting form rest moves vertically upwards with a constant acceleration $\frac{g}{2}$.

After time *T* a part of the shuttle is released from the shuttle and it moves vertically downwards under the gravity so as to fall on the ground. When the released part is at its maximum height, engine of the space shuttle stops suddenly and falls vertically down under the gravity.

Draw velocity - time curves for the motions of the space shuttle and the released part of the shuttle and the remaining part of the shuttle in a same diagram until they reach to the ground from the initial moment.

Hence show that the velocity of the shuttle when the part is released is $\frac{gT}{2}$ and the maximum height of the released part is $\frac{3gT^2}{8}$.

Further show that the velocity of the shuttle is $\frac{3gT}{4}$ when the engine stops. And also show that the maximum height reached by the shuttle is $\frac{27gT^2}{32}$.

Show that the velocities of the released part and the shuttle from the initial moment when they fall on the ground are $\frac{\sqrt{3}}{2}gT$ and $\frac{3\sqrt{3}}{4}gT$ respectively.

(b) A destroyer D sails due east with uniform speed $u \, km \, h^{-1}$. Another ship S sails in the direction α north of east at a constant speed $v \, km \, h^{-1} \, (v \cos \alpha > u)$. At a certain moment, the ships S is at a distance $a \, km$ south of D.

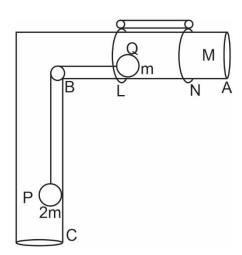
Draw the velocity triangles for the relative motions of S and D. Also draw the locus of the ship relative to D. Show that the shortest distance between the ship S and D is , $\frac{a (v \cos \alpha - u)}{\sqrt{v^2 + u^2 - 2uv \cos \alpha}} km$

Further show that the time taken to reach this closest moment from the moment where S is at a distance $a \ km$ south of D is $\frac{av \sin \alpha}{v^2 + u^2 - 2uv \cos \alpha}$ hours.

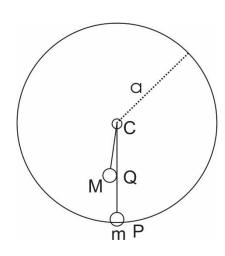
12) (a) A thin smooth tube of mass *M* is bent at *B* so as to from a right angle. Part *AB* is horizontal and it is free to move through two smooth rings *L* and *N*. *BC* is vertical. Two particles *P* and *Q* of masses 2*m* and *m* are connected by a light inextensible string passing over a smooth pulley fixed at *B*. Initially particle *Q* is placed at a point in tube *AB* and particle *P* is hung vertically inside *BC*. Then the system is released gently with the string taut.

Write down the equations of motion for particle P along BC, for particle Q along AB and for the system along BA. Show that the acceleration of the tube is $\frac{2mg}{3M+8m}$

Also show that the acceleration of each particle relative to the tube is, $\left(\frac{M+3m}{3M+8m}\right) 2g$ and the acceleration of the particle *P* relative to earth is, $\left(\frac{2g}{3M+8m}\right) \sqrt{M^2 + 10 m^2 + 6Mm}$.



b) A smooth bead P of mass m is thread to a circular wire of radius a fixed in a vertical plane. The bead is free to move along the wire. One end of a light inextensible string passing through a smooth ring at the center C, is connected to the bead P and the other end of the string is connected to a particle Q of mass M. Initially the bead P is placed at the lowest point and projected horizontally with a velocity of \sqrt{kga} (k > 1) so that the bead is in a circular motion along the wire.



Show that the speed v of the bead P, when the string PC makes an acute angle θ with the downward

vertical is given by $v^2 = kga - 2ga + 2ga\cos\theta$ and the reaction R on the bead P from the wire is given by $R = mg\left(k - 2 + 3\cos\theta - \frac{M}{m}\right)$.

Taking k = 6, if m < M < 7m show that the reaction on the bead by the wire is disappeared at a certain moment.

One end of a light elastic string of natural length l is connected to a particle P of mass m and the other end is connected to a fixed point at O.

When the particle is suspended in equilibrium the extension of the string is l. Show that the modulus of elasticity is mg.

Then the particle is placed at O and released gently. Show that the velocity of the particle is $\sqrt{2gl}$ when it falls a distance l vertically downwards. When the length of the string x(x > l) is from O, show that the equation of motion of the particle is given by $-\frac{9}{l}(x-2l) = \ddot{x}$ with the usual notation.

Also assuming that the velocity of the particle is given by $\dot{x}^2 = w^2 (A^2 - x^2)$; A > 0 (Constant) find the value of A.

Show that the time taken by the particle to reach the point 0 again is, $2\sqrt{\frac{l}{g}}\left\{\sqrt{2} + \pi - \cos^{-1}\left(\frac{1}{\sqrt{3}}\right)\right\}$

14) (a) \underline{a} and \underline{b} are, two non-zero, non-parallel vectors. Prove that $\alpha=0$ and $\beta=0$ is the necessary and sufficient condition for $\alpha\underline{a}+\beta\underline{b}=0$. Here α and β are scalars.

In the parallelogram OACB, $\overrightarrow{OA}=\underline{a}$ and $\overrightarrow{OB}=\underline{b}$. D is a point on OA such that OD:DA=1:2. BD and AC intersect at X. λ and μ are two scalars such that $OX=\lambda OC$ and $OX=\mu BD$. Find the values of λ and μ and show that BX:XD=3:1 and OX:XC=1:3.

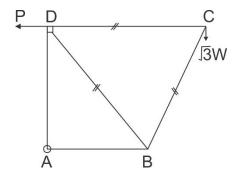
(b) In the rectangle ABCD. AB = a, AD = 2a. M is the mid point of AD. Forces P, 2P, 4P, 6P, $3\sqrt{2}P$ and $\sqrt{5}P$ act along the sides CB, DA, BA, CD, MB and DB in the direction of the order of the letters respectively. If the system is reduced to a couple and a single force acting at A, find the magnitude and the direction of the single force. Show that the magnitude of the couple is 6Pa and find the sense of it.

8

15) (a) A rhombus ABCD is formed of four uniform rods AB, BC, CD, and AD each of length 2a and weight w, smoothly jointed at their ends. The rhombus is suspended from A and a light inextensible string is connected to the points L and M on the rods AB and BC respectively. Here $AL = CM = \frac{a}{2}$.

The string LM and AC are vertical and the system is in equilibrium in a vertical plane with the vertex A is above C. Given that $B\hat{A}D = B\hat{C}D = 60^{\circ}$.

- (i) Find the reaction at C and show that its inclination to the horizontal is $tan^{-1}(2\sqrt{3})$.
- (ii) Show that the tension of the string LM is $\frac{8w}{3}$.
- (iii) Find the magnitude and the direction of the reaction at B.
- (b) Five light rods AB, BC, CD, BD and AD are smoothly jointed at their ends to from the framework shown in the figure. Given that BC = BD = CD = 2a. The framework is smoothly hinged at A and weight $\sqrt{3}w$ is hung at C. A horizontal force P applied at D, keeps the frame work in a vertical plane such that AB and DC horizontal and AD vertical.

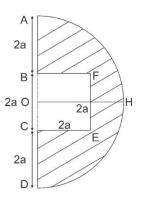


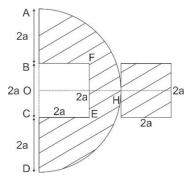
- (i) Find the value of P.
- (ii) Find the reaction at A and its inclination to the horizontal.
- (iii) Draw stress diagrams for each joint on the same figure, using Bow's notation. Hence find the stresses of rods indicating whether they are tensions or thrusts.
- Show that the center of mass of a semi circular lamina of radius a and center 0 is at a distance $\frac{4a}{3\pi}$ from 0.

A square *BFEC* of side 2a is removed symmetrically about *OH* from a uniform semi-circular lamina *AHD* of radius 3a. Show that the center of mass of the remaining part is at a distance $\frac{28 a}{9\pi - 8}$ from *O* on the axis of symmetry.

Then the removed square is attached at H as shown in the figure.

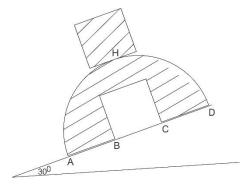
Show that the center of mass of the this object is on the axis of symmetry at a distance $\frac{2a}{3\pi}$ from O.





If the new lamina rests on a rough plane inclined at an angle 30^{0} to the horizontal and AB and CD are on the line of greatest slope, show that $\mu \geq \frac{1}{\sqrt{3}}$.

Here μ is the coefficient of friction between the inclined plane and the lamina.



- 17) (a) Let A and B be any two events of the sample space Ω . Define each of following events.
 - (i) A and B are mutually exclusive events.
 - (ii) A and B are exhaustive events.
 - (b) Given that A, B and C are three mutually exclusive and exhaustive events of the sample space Ω . If $P(A) = 2a^2$, P(B) = 2a and P(C) = 8a 1, find the value of a.
 - (c) Let A and B are any two events of the sample space Ω . Show that,
 - (i) $P(A) = P(A \cap B) + P(A \cap B')$
 - (ii) $P(A \cup B) = P(A) + P(B) P(A \cap B)$ Here, B' is the complement of event B. If $P(A') = \frac{1}{4}$, $P(B) = \frac{1}{2}$, $P(A \cap B') = \frac{2}{5}$, Find $P(A \cap B)$, $P(A \cup B)$, $P(A' \cap B)$, $P(A' \cup B)$ and $P(A' \cup B')$

and one blue ball without replacement. Find the probabilities of,

- (d) A biased die which has $\frac{3}{5}$ of probability of getting head is tossed. If the head is obtained, then 2 balls are taken out randomly from a box A containing 3 red balls and 2 blue balls which are identical without replacement.

 If the tail is obtained, then two balls are taken out randomly from a box B containing 2 red balls
 - (i) Obtaining 2 red balls.
 - (ii) Obtaining only one red ball when tail is obtained.

NWP Second Term Test - Grade 13 - 2020 Combined Mathematics I.

(01) When
$$p=1$$

LHS=1 RHS= $\frac{15[3\times 1-1]}{2}$

=1

LHS=RHS

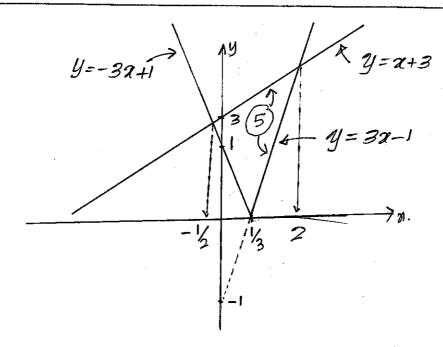
The result is true for $p=1$

Assume that the result is true for $p=1$
 $p=1$

it is also true for n=pezt. then

it is also true for n=p+1. by using the

principle of mathematical induction. The result is true
for all next.



$$-3x+1=x+3$$

$$4x=-2$$

$$x=-1/2$$

$$=$$

$$3x-1=x+35$$

$$2x=4$$

$$x=2$$

:. Solution is
$$\alpha \in (-\infty, -2\frac{1}{2}) \cup (0, \infty) (5)$$

(03)
$$a \xrightarrow{1/2} \frac{4\sqrt{2} - (10S\alpha + SIm)^5}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} \left\{ \frac{1}{J_2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}} \right\}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{4\sqrt{2} - 4\sqrt{2} (10S\alpha + \frac{1}{J_2} SIm)^{\frac{5}{2}}}{1 - SIn2\alpha}$$

$$= a \xrightarrow{1/2} \frac{1}{J_2} \frac{1}{J_2$$

(04)
$$U_{r} = \frac{r}{(r+1)!}$$

$$f(r) - f(r+1) = \frac{1}{r!} - \frac{1}{(r+1)!}$$

$$= \frac{r+1-1}{(r+1)!}$$

$$= \frac{r}{(r+1)!}$$

$$= \frac{r}{(r+1)!}$$

$$= \frac{r}{(r+1)!}$$

$$= \frac{r}{(r+1)!}$$
When $r=1$ $U_{1} = f(1) - f(2)$

$$r=2 \quad U_{2} = f(2) - f(3)$$

$$r=3 \quad U_{3} = f(3) - f(4)$$

$$r=1 \quad U_{n-1} = f(n-1) - f(n)$$

$$r=n \quad U_{n} = f(n) - f(n+1)$$

$$= \frac{r}{r} \quad U_{r} = f(1) - f(n+1)$$

$$= \frac{r}{r} \quad U_{r} = \frac{r}$$

(05)
$$x = (t+1)^2 t$$

 $y = \frac{1}{2}t^3$
 $y = \frac{1}{2}t^3$
 $y = \frac{1}{2}$

$$a = (t+1)^{2}t$$

$$\frac{da}{dt} = (t+1)^{2} + t \cdot 2(t+1)^{2}$$

$$= (t+1)[(t+1) + 2t] \quad (5)$$

$$\frac{dy}{dx} = \left(\frac{dy}{dt}\right) \left(\frac{dt}{dx}\right)$$

$$=\frac{3(2t)^{2}(3t+1)}{(4+1)(3t+1)}=\frac{3t^{2}}{2(t+1)(3t+1)}$$

$$m_1 = \left(\frac{dy}{dx}\right)_{t=2}$$

$$= \frac{3\times4}{2\times3\times7}$$

$$\frac{2}{4}(m_g) = -1$$

$$m_2 = \frac{7}{27} (5)$$

y= 1/2 +3

 $\frac{dy}{dt} = \frac{3}{2}t^2$

.: Equation of the normal

$$\frac{y-4}{2-18} = -\frac{7}{2}$$
 (5)

$$2y + 7a = 134$$

(06) The area is given by
$$\int_{0}^{0} y dx - \int_{0}^{1} y dx = \int_{0}^{1} y$$

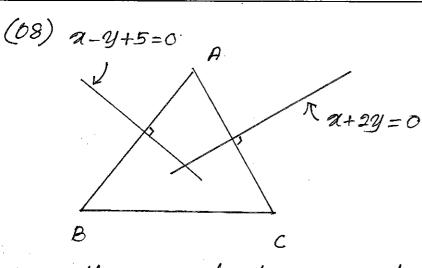
Let $p(2t^2, 4t)$ be any Point on the parabola then $(cp)^2 = (2t^2)^2 + (4t+6)^2$ $= 4t^4 + 4(2t+3)^2$

$$f(t) = 4t^{2} + 4(2t+3)^{2} = 16(t) = 16t^{3} + 16(2t+3)$$

$$= 16(t+3) + 2t+3$$

$$= 16(t+1)(t^{2} + t+3)$$

$$= 16(t+1)\left\{(t-\frac{1}{2})^{2} + \frac{11}{4}\right\} = 16(t+1)\left\{(t-\frac{1}{2})^{2} + \frac{11}{4}\right\} = 16(t+1)\left\{(t+\frac{1}{2})^{2} + \frac{11}{4}\right\} = 16(t+1)\left\{(t+\frac{1}{2}$$



let the co-ordinates of B be (dip).

Since Co-ordinates of A are (1,-2) .. the slope of AB = B+2

The equation of the perpendicular bisector of AB 15 a-y+5=0

$$\Rightarrow \frac{\beta+2}{d-1} \cdot 1 = -1$$

$$\beta+2 = -d+1$$

$$d+\beta = -1 \longrightarrow 0 \quad \boxed{5}$$

Also the midpoint of AB lies on a-y+5=0

$$\Rightarrow \left(\frac{\alpha+1}{2}\right) - \left(\frac{\beta-2}{2}\right) + 5 = 6$$

 $d+1-\beta+2+10=0$

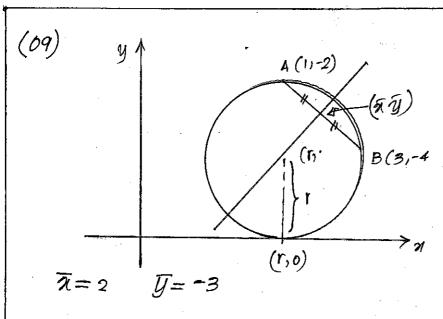
Dand 2 2d = -14

$$d = -7$$

Similarly the co-ordinates 01 c are (#, 2) (5)

: the equation of the line BC PS $(y-6)=\frac{(2/5-6)}{(1/5+7)}(x+7)$

$$14x + 23y = 40.5$$



$$(\overline{A}, \overline{Y}) \equiv (2, -3)$$

:. +he slope of
$$AB = \frac{-4+2}{3-1} = \frac{-2}{2} = -1$$

: The equation of the perpendicular bisector of AB is

$$\frac{y+3}{x-2} = +1$$

$$\frac{y+3}{1} = \frac{x-2}{1} = t$$

$$y=t-3 \quad \text{and} \quad x=t+2$$

t=-7 or t=1 5

: Centre of the Circle $\equiv (t+2, t-3)$

$$(t+2-1)^{2} + (t-3+2)^{2} = t-3.$$

$$(t+1)^{2} + (t-1)^{2} = (t-3)^{2}$$

$$t^{2} + 2t + 1 + t^{2} - 2t + 1 = (t-3)^{2}$$

$$2t^{2} + 2 = t^{2} - 6t + 9$$

$$t^{2} + 6t - 7 = 6$$

$$(t+7)(t-1) = 0$$

:. Centre = (-10,-5)

radius = 10

:. equation is $(2+10)^{2}+(y+5)^{2}=10^{2}/(5)$ or

centre = (2,3)

radius = 2 $(2+2)^{2}+(y-3)^{2}=2^{2}$ $(2+2)^{2}+(y-3)^{2}=2^{2}$

(10) Sinba+ cos 4x+2 =0; OEX < 24 ie. 35/02n-45/032x + 1-25/022x+2=00 -4512x-2512x+35102x+3=0 Cet Sin 2x = y $-4y^{3} - 2y^{2} + 3y + 3 = 0$ $) y^{2} 8 \ln 2x$ when yz1, -4-2+3+3 = 0 : (y-1) 15 a factor (5) (y-1) (-4y2+Ag-3) = 0 comparing y's coefficients. $-2 = +9 + A \Rightarrow A = -6$ Cet gar) = -4 y2-6 y-3 $2-4(y^2+3y+3)$ = -4 ((y+2)2+2-16) =-9 [(y+34) + 3) \$ 6 onlyappeal solution. 15 at y21 6 i.e. sm22=1= s102x=510th : 2x = nt + (-1) 1/2 5 2 2 ng + (-1) t/a for n=1 x = T/4 = T/4 / x= # + T/q = 5 T/4/1 (5) x 2 3T/2 - T/4 = 5 T/4

(11) (a) (i) $x^2 - 3 + k(2x + 3) = 0$ $x^2 + 2kx + 3(k-1) = 0 - \beta$ (k-1)(k+1) = 3(k-1) $\Rightarrow (k-1)(k+1-3) = 0$ (k-1)(k-2) = 0k = 1 or k = 2 $\frac{1}{x+1} + \frac{1}{x-1} = \frac{1}{c}$; $x \neq \pm 1$, $c \neq 0$ (ii) $c(x-1+x+1) = x^2-1$ 20x = x2-1 $x^2 - 2Cx - 1 = 0$ (5) $\Delta = (-2c)^2 An (n(1)) (5)$ $= 4C^2 + 4$ = 4 (C2+1) > 0 always when cis real (5) .: The quadratic equation has distinct roots. (b) (i) $f(\alpha) = x^5 - 3x^4 + 2x^3 - 2x^2 + 3x + 1$ $f(-1) = -1 -3 -2 -2 -3 + 1 = -10 \neq 0$.: (a+1) is not a factor of fac). (5) $f(1) = 1 - 3 + 2 - 2 + 3 + 1 = 2 \neq 0$ -: (x-1) is also not a factor of foo 2) neither (x+1) nor (x-1) is a factor of few

$$\frac{q(x)}{(x-1)} = (x-1)(x^2-2x-1)$$

$$= (x-1)(x^2-3x+1-1-1)$$

$$= (x-1)(x-1)^2-J_2^2 = (x-1)(x-1-5)(x-1+52) = 0$$

$$\frac{(x^2+1)(x-1)}{(x-1)} = (x-1)(x-1-5)(x-1+52) = 0$$

$$\frac{(x^2+1)(x-1)}{(x-1)} = (x-1)(x-1-5) = 0$$

$$\frac{(x^2+1)(x-1)}{(x-1)} = (x-1)(x-1-5) = 0$$

$$\frac{(x^2+1)(x-1)}{(x-1)} = (x-1)(x-1-5) = 0$$

$$\frac{(x^2+1)(x-1)}{(x-1-5)} = (x-1)(x-1-5) = 0$$

$$\frac{(x-1)}{(x-1-5)} = (x-1-5) = 0$$

$$\frac{(x-1)}{(x-1$$

(b) to prove that
$$1+n^2+n^4=(1+n^2)^2-n^2$$

RHS = $1+2n^2+n^4-n^2$

= $1+n^2+n^4$

= $1+n^2+n^$

$$= \frac{1}{r^2 + r + 1 \cdot (5)}$$

$$U_{r} = \frac{1}{2} \left(f_{(r)} - f_{(r+1)} \right) \left(\frac{1}{5} \right)$$

$$2 U_{r} = f_{(r)} - f_{(r+1)}$$

$$2 \int_{r=1}^{n} U_{r} = f_{(r)} - f_{(r)} \left(\frac{1}{5} \right)$$

$$= f_{(r)} - f_{(r+1)} \left(\frac{1}{5} \right)$$

$$= \frac{1}{r-1} U_{r} = \frac{1}{2} \left(\frac{1}{1+1^{2}-1} - \frac{1}{n^{2}+n+1} \right) \left(\frac{1}{5} \right)$$

$$= \frac{1}{2} \frac{n^{2}+n+1}{n^{2}+n+1} = \frac{n(n+1)}{2(n^{2}+n+1)} \left(\frac{5}{5} \right)$$

(13)
$$a \cdot (osa + (os(a+p) + cos(a+ep) + ... + cos(a+(n-1)p)$$

$$= \frac{(os\left\{\alpha + \left(\frac{n-1}{2}\right)p\right\} \cdot Sin\left(\frac{np}{2}\right)}{Sin\left(\frac{p}{2}\right)}$$

When
$$n=1$$

$$LHS = (oSa)$$

$$RHS = \frac{(oS(\alpha+o))Sin(\frac{B}{2})}{Sin(\frac{B}{2})}$$

Pake any pezt

Assume that the result is true for n=p.

$$(\cos \alpha + \cos(\alpha + \beta) + \cos(\alpha + 2\beta) + \dots + \cos(\alpha + (P-1)\beta)$$

$$(\cos \left\{\alpha + \left(\frac{P-1}{2}\right)\beta\right\} \sin\left(\frac{P\beta}{2}\right)$$

When n=p+1

$$\frac{(os \alpha + cos (\alpha + \beta) + \dots + cos \{\alpha + (p-1)\beta\} + cos \{\alpha + p\beta\} = 0}{from G}$$

$$\frac{\cos\left\{d+\left(\frac{P-1}{2}\right)\beta\right\}\sin\left(\frac{PB}{2}\right)}{\sin\left(\frac{B}{2}\right)} + \cos\left(d+P\beta\right)$$

$$= 2\cos \left\{\alpha + \left(\frac{p-1}{2}\right)\beta\right\} \sin \left(\frac{p\beta}{2}\right) + 2\sin \left(\frac{\beta_{2}}{2}\right) \cos \left(\alpha + p\beta\right)$$

$$= 2\sin \left(\frac{\beta_{2}}{2}\right) + 2\sin \left(\frac{\beta_{2}}{2}\right) \cos \left(\alpha + p\beta\right)$$

$$= \sin \left\{\alpha + p\beta - \frac{\beta_{2}}{2}\right\} - \sin \left(\alpha - \frac{\beta_{2}}{2}\right) + \sin \left\{\alpha + p\beta + \frac{\beta_{2}}{2}\right\}$$

$$= -\sin \left\{\alpha + p\beta - \frac{\beta_{2}}{2}\right\}$$

25in (B/2)

$$= \frac{\cos\left(\alpha + \frac{PB}{2}\right) \sin\left(p + 1\right)B}{\sin\left(\frac{B}{2}\right)}$$

$$= \frac{5 \sin\left(\frac{B}{2}\right)}{\sin\left(\frac{B}{2}\right)}$$

If the result is true for $n=p\in 2^{t}$ then it is also true for n=p+1 therefor by using the principle of mathematical induction the result is true for all $n\in 2^{t}$.



(b)
$$\frac{12!}{2!} = 239500800 (5)$$

$$J \frac{10!}{2!} = 1814400 (1)$$



1632 (5)



(14) (a)
$$y = f(x) = \frac{16(x+1)}{(x-1)^2(3x+1)^4} = \frac{16(x+1)}{3x^3 - 5x^2 + x + 1}$$

$$f'(x) = 16[(x-1)^2(3x+1) \times 1 - (x+1)(9x^2 - 10x + 1)]$$

$$(x-1)^4(3x+1)^2$$

$$= 16(x-1)(3x+1) - (x+1)(9x-1)$$

$$(x-1)^3(3x+1)^2$$

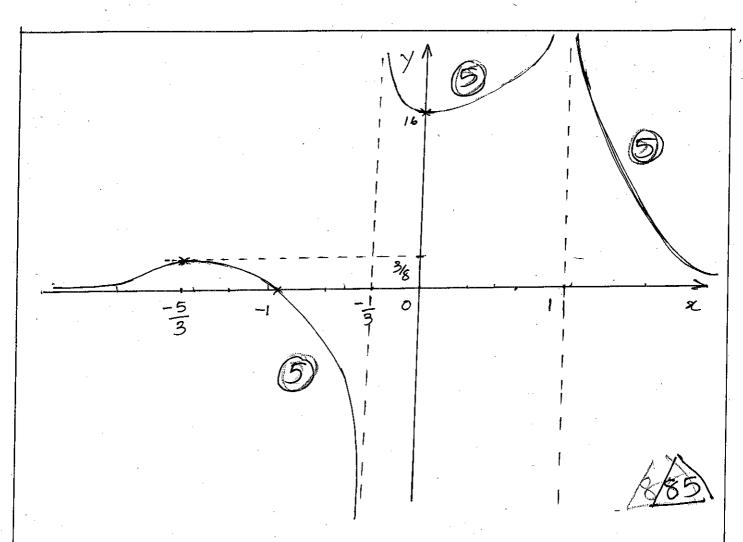
$$= \frac{16x(-2x)(3x+5)}{(x-1)^3(3x+1)^2}$$

$$= \frac{-32x(3x+5)}{(x-1)^3(3x+1)^2}$$

Vertical asymptotes. x=1, $x=-\frac{1}{3}$ \bigcirc Horizonta asymptote. $x\to\pm\infty$, y=0 \bigcirc The point horizontal asymptote intersects the curve. When y=0, $z=-1 \Rightarrow (-1,0)$ \bigcirc \bigcirc

Turning points. when $f(\alpha) = 0$, $\alpha = \frac{-5}{3}$ or $\alpha = 0$ y = 16Then $y = \frac{3}{8}$

	-00<2<5	-5く欠く-1	글 <x<0< th=""><th>0 < % < 1</th><th>122100</th></x<0<>	0 < % < 1	122100
sign	+-	+ + - +	+ +	- + - +	4 + + + + + + + + + + + + + + + + + + +
f(x)	(+)	(-)	(-)	(+)	(A)
	-			-	w \
					.



(b) (i)

O

A

P

B

Let
$$AP = x m$$

But $A = 4x^2$

$$OP = 216 \text{ m}, OG = h$$

Area ABCD = A

Volume $V = \frac{1}{3} Ah$
 $h^2 = (356)^2 - 2e^2$
 $= 9 \times 6 - \frac{A}{4}$
 $h^2 = 54 \times 4 - A = \frac{216 - A}{4}$
 $\therefore V = \frac{1}{3} A \times \frac{216 - A}{4}$
 $V = \frac{A}{6} \sqrt{216 - A}$

(ii)
$$V = \frac{1}{6} A (216-A)^{1/2}$$

$$\frac{dV}{dA} = \frac{1}{6} \left[A \cdot \frac{1}{2} (216-A)^{1/2} (216-A)^{1/2} \times 1 \right] (10)$$

$$= \frac{1}{6} \left(\frac{-4}{2\sqrt{216-A}} + \sqrt{216-A} \right)$$

$$= \frac{1}{6} \cdot \frac{-4}{2\sqrt{216-A}} + \frac{1}{2\sqrt{216-A}} = \frac{1}{4} \cdot \frac{144-A}{\sqrt{216-A}} (5)$$

When $\frac{dV}{dA} = 0$, $A = 144 \text{ m}^2 (5)$

OLA LI44 $A = 144$ 144 LA Laib

Sign of $\frac{dV}{dA}$

Vis maximum, when $A = 144 \text{ m}^2$

(b) Height $A = \frac{1}{2} = \frac{1}{4} = \frac{1}$

(15) a.
$$\frac{1}{(1-z)(1-2z)} = \frac{A}{(1-z)} + \frac{B}{(1-2z)}$$

$$= A(1-2z) + B(1-2z)$$
Compairing C
$$coefficient of 2, -2A - B = 0 - 0$$

$$constants, A + B = 1 - 0$$

$$0 + 0 \Rightarrow -A = 1 \Rightarrow A = -1 = 0$$

$$0 \Rightarrow -1 + B = 1 \Rightarrow B = 2 = 0$$

$$\frac{1}{(1-2)(1-2z)} = \frac{-1}{1-z} + \frac{2}{1-2z} = 0$$
When $t = \sin x$, $\frac{dt}{dx} = \cos x$. $\frac{dx}{dx} = \cos x$

$$= \frac{1}{4} \int \frac{1}{1-t^2} dt + \frac{1}{4} \int \frac{1}{(f_3)^2 - t^2} dt$$

$$= \frac{1}{8} \ln \left| \frac{1+t}{1-t} \right| + \frac{1}{4\sqrt{2}} \ln \left| \frac{1+J_5t}{1-J_5t} \right| + C$$

$$= \frac{1}{8} \ln \left| \frac{1+J_5t}{1-s} \right| + C$$

$$= \frac{1}{8} \ln \left| \frac{1+J_5t}{1-s} \right| + C$$

$$= \frac{1}{8} \ln \left| \frac{1+J_5t}{1-J_5t} \right| + C$$

$$= \frac{1}{8} \ln \left| \frac{1+J$$

$$= \int_{a}^{b} \int_{a-a}^{b-x} dx = \int_{a}^{b} \int_{a-a}^{b-x} dx$$

$$= \int_{a}^{b} \int_{b-2}^{a-a} dx + \int_{a}^{b-x} \int_{a-a}^{b-x} dx$$

$$= \int_{a}^{b} \int_{-a}^{b-a} \int_{-a}^{b-x} dx$$

$$= \int_{a}^{b} \int_{-ab+(a+b)}^{b-x} dx$$

$$= (b-a) \int_{a}^{b-a} \int_{-a-2}^{b-a} \int_{a}^{b-a} dx$$

$$= (b-a) \left[\sin^{-1}(1) - \sin^{-1}(-1) \right]$$

$$= \int_{a}^{b-a} \int_{a}^{b-a} \int_{a}^{b-a} dx$$

$$= (b-a) \left[\sin^{-1}(1) - \sin^{-1}(-1) \right]$$

$$= \int_{a}^{b-a} \int_{a}^{b-a}$$

$$= \frac{e^{3x}}{3} \sin 4x - \frac{4}{3} \left[\frac{e^{3x}}{3} \cos 4x + \int \frac{e^{3x}}{3} \sin 4x \frac{dx}{dx} \right]$$

$$\int e^{3x} \sin 4x \, dx = \frac{e^{3x}}{3} \sin 4x - \frac{4}{9} e^{3x} \cos 4x - \frac{16}{9} \int e^{3x} \sin 4x \, dx$$

$$\frac{25}{9} \int e^{3x} \sin 4x \, dx = \frac{e^{3x}}{3} \sin 4x - \frac{4}{9} e^{3x} \cos 4x$$

$$\frac{25}{9} \int e^{3x} \sin 4x \, dx = \frac{e^{3x}}{3} \sin 4x - 4 e^{3x} \cos 4x$$

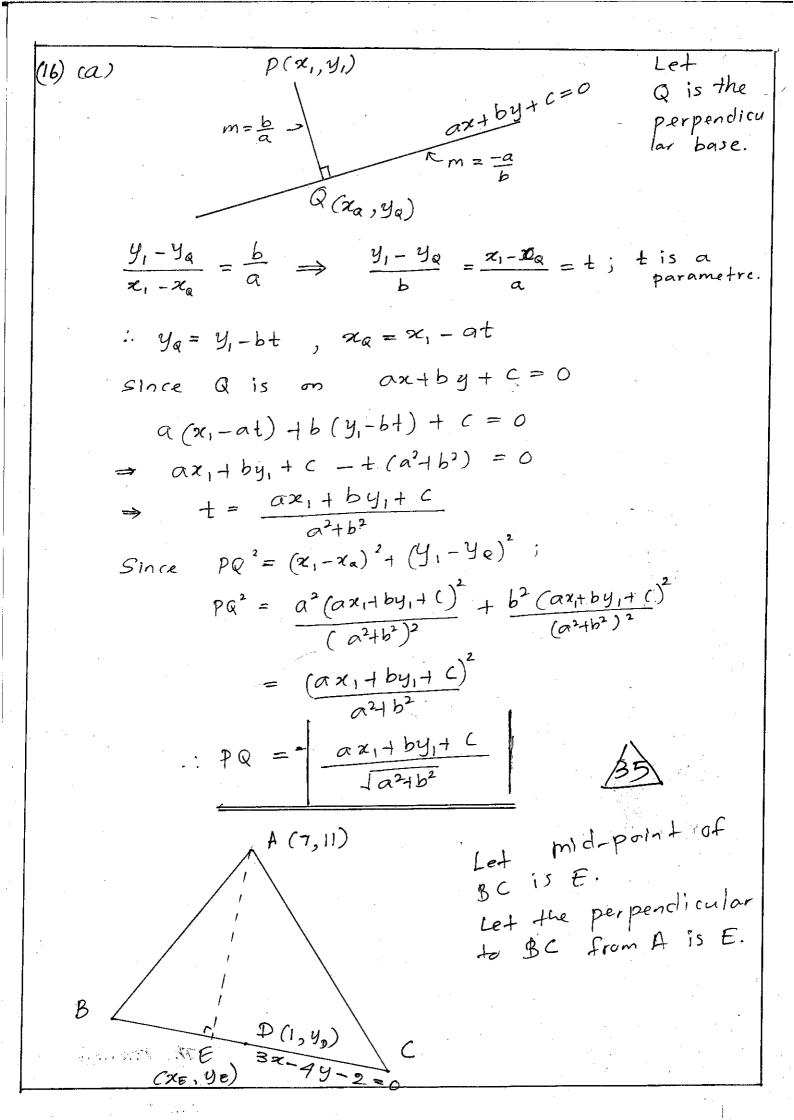
$$\frac{25}{9} \int e^{3x} \sin 4x \, dx = \frac{e^{3x}}{3} \sin 4x - 4 e^{3x} \cos 4x$$

$$\frac{25}{9} \int e^{3x} \sin 4x \, dx = \frac{e^{3x}}{3} \sin 4x - 4 e^{3x} \cos 4x$$

$$\frac{25}{9} \int e^{3x} \sin 4x \, dx = \frac{e^{3x}}{3} \sin 4x - 4 e^{3x} \cos 4x$$

$$\frac{25}{9} \int e^{3x} \sin 4x \, dx = \frac{e^{3x}}{3} \sin 4x - 4 e^{3x} \cos 4x$$





Since Q is on BC,
$$3 \times 1 - 4 \times y_b - 2 = 0$$

$$\Rightarrow y_b = \frac{1}{4}$$
Also
$$\frac{76 + 2c}{2} = 1 \Rightarrow x_b + x_c = 2 - 0$$

$$\frac{76 + 7}{2} = \frac{1}{4} = 96 + 9c = \frac{1}{2} - 0$$
But $AE = \left| \frac{3 \times 7 - 4 \times 11 - 2}{3^2 + 4^2} \right| = 5$

$$\therefore P = DC = 6 \text{ units.}$$

$$\therefore P = DC = 6 \text{ units.}$$

$$\therefore P = DC = 6 \text{ units.}$$

$$\therefore P = \frac{4}{3} \times p + \frac{2}{3} - 1 = \frac{4}{3} \times p + \frac{2}{3}$$

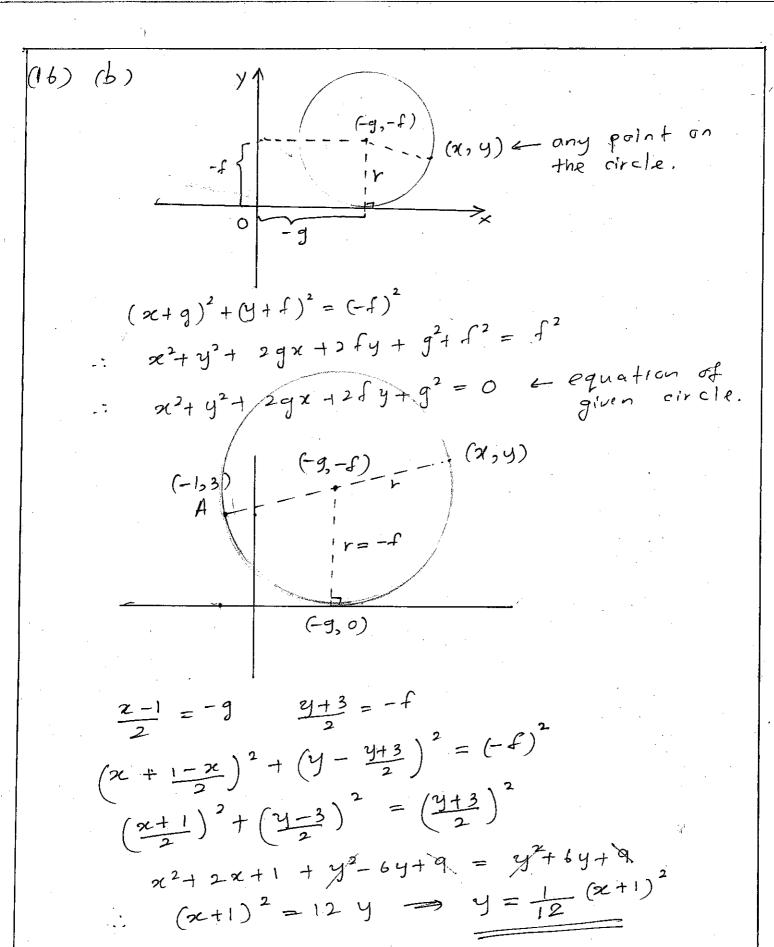
$$\therefore P = \frac{4}{3} \times p + \frac{2}{3} - 1 = \frac{4}{3} \times p + \frac{2}{3}$$

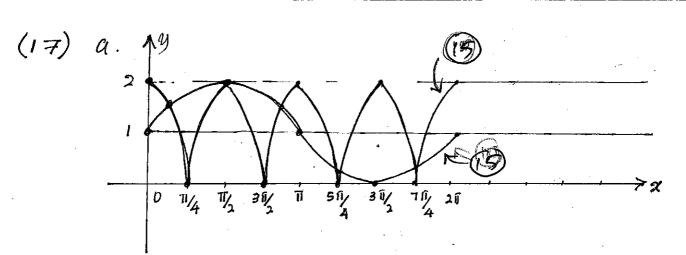
$$\therefore P = \frac{4}{3} \times p + \frac{2}{3} - 1 = \frac{4}{3} \times p + \frac{2}{3}$$

$$\therefore P = \frac{4}{3} \times p + \frac{2}{3} - 1 = \frac{4}{3} \times p + \frac{2}{3}$$

$$\therefore P = \frac{4}{3} \times p + \frac{2}{3} - 1 = \frac{4}{3} \times p + \frac{2}{3} = \frac{4}{3} \times p + \frac{2}{3}$$

$$\therefore P = \frac{4}{3} \times p + \frac{2}{3} + \frac{1}{4} = \frac{4}{3} \times p + \frac{2}{3} \times p + \frac{2}{3} = \frac{4}{3} \times p + \frac{2}{3} \times p + \frac{2}{3}$$







Let
$$\frac{SinB}{a} = \frac{SinB}{b} = \frac{SinC}{c} = K$$

$$\frac{SnA}{a} = k \implies SnA = kq$$

$$\frac{SinB}{b} = K \Rightarrow SinB = Kb$$

$$\frac{Sinc}{c} = k \implies Sinc = kc$$

$$\cos a = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos B = \frac{a^2 + (^2 - b^2)}{2a($$

$$cosc = \frac{a^2 + b^2 - c^2}{2ab}$$

$$\frac{Sin(A-B)}{Sin(A+B)} = \frac{a^2 b^2}{a^2 + b^2}$$

$$\frac{Sin(A-B)}{Sin(A+B)} = \frac{a^2 b^2}{a^2 + b^2}$$

$$\frac{Sin(A-B)}{Sin(A+B)} = \frac{a^2 b^2}{a^2 + b^2}$$

$$\frac{Sin(A+B)}{Sin(A+B)} = \frac{a^2 b^2}{a^2 + b^2}$$

$$\frac{2a^2 + c^2 b^2}{2ac} = \frac{a^2 b^2}{a^2 + b^2}$$

$$\frac{a^2 + c^2 b^2 - b^2 - c^2 + a^2}{a^2 + c^2 - b^2} = \frac{a^2 b^2}{a^2 + b^2}$$

$$\frac{a^2 + c^2 - b^2 + b^2 + c^2 - a^2}{a^2 + b^2}$$

$$\frac{a^2 + c^2 - b^2 + b^2 + c^2 - a^2}{a^2 + b^2}$$

$$\frac{a^2 + b^2 - c^2}{a^2 + b^2}$$

$$\frac{a^2 + c^2 - b^2}{a^2 + c^2}$$

$$\frac{a^2 + c^2 - b^2}{a^2 + b^2}$$

$$\frac{a^2 + c^2 - b^2}{a^2 + b^2}$$

$$\frac{a^2 + b^2}{a^2 + b^2}$$

$$\frac{a^2 + b^2}{a^2 + b^2}$$

$$\frac{a^2 + c^2 - b^2}{a^2 + b^2}$$

$$\frac{a^2 + b$$

 $32 = -\sqrt{3} + \sqrt{3} \times 2x^{2}$ $2\sqrt{3}x^{2} - 3x - \sqrt{3} = 0$ $2 = 3 + \sqrt{9 + 4 \times 2\sqrt{3}x/3}$ $2 + \sqrt{3} = \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} + \sqrt{3} = \sqrt{3} + \sqrt{3}$ $2 + \sqrt{3} = \sqrt{3} + \sqrt{3} + \sqrt{3} = \sqrt{3}$

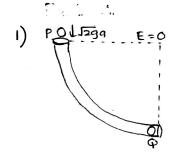
MARKING SCHEME

G.C.E (Advance Level) - 1 March 2020

Grade 13 - Term Test I

COMBINED MATHEMATICS I

PARTA



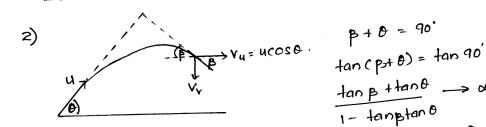
Applying the Law of conservation of energy for P,

$$0 + \frac{1}{2} \text{ m. } 2ga = -mga + \frac{1}{2} \text{ mv}^2$$
 (10)
$$2ga = -2ga + v^2$$

$$v^2 = 499$$
 (5)

Applying the law of conservation of energy,





$$1 - tanp tan \theta = 0$$

$$tan \theta = 1$$

$$tanptan \theta = 1 (5)$$

$$V = u + at$$

$$V_r = u \sin \theta - gt$$

$$\frac{v_r = u\sin\theta - gc}{v_r = gt - u\sin\theta} = \frac{v_r}{v_u} = \frac{gt - u\sin\theta}{u\cos\theta} = \frac{5}{5}$$

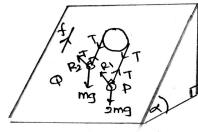
from (),
$$(\frac{gt-u\sin\theta}{u\cos\theta})$$
 fan $\theta = 1$ (5)

$$\left(\frac{gt - usin\theta}{ucoso}\right)\left(\frac{sin\theta}{\cos\theta}\right) = 1$$

gt sine -
$$u sin^2\theta = u cos^2\theta$$

gt sine = $u (sin^2\theta + cos^2\theta)$
 $t = \frac{u}{gsin\theta}$

3)



Applying F=ma 1/2, for P, 2mg sin d-T = 2mf -0

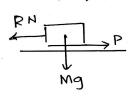
Applying F=ma (x) for O T-mg sind = mf -2 (E)

1 + 2, mg sind = 2mf $f = \frac{g \sin \alpha}{3}$

From 3,

 $T = mg \sin \alpha + \frac{mg \sin \alpha}{2}$

T = 4 mg sind (5)

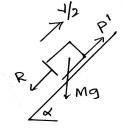


For car,
$$H = PY$$

$$b = \frac{\Lambda}{H \times 10^3} \text{ M }$$

$$P-R=0$$

$$P=R=\frac{H\times 10^3}{V} N (5)$$



For the motion on the inclined plane H = PV

$$H = PV$$
 $H \times 10^3 = P^1 \frac{V}{2}$
 $P^1 = 2H \times 10^3 \text{ M. (5)}$

Applying & F=ma

$$p'-R-Mg$$
 sind = Ma (5)

$$P^{1}-R-Mg \sin x$$

$$2Hx10^{3}-\frac{Hx10^{3}}{V}-Mg \sin x=Mg$$

$$q = \left(\frac{H \times 10^3}{MV} - 9 \sin \alpha\right) \frac{1}{MS}$$

$$\cos \theta = \frac{3}{5}$$

Applying the Law of Conservation of energy

$$\frac{1}{2}mv^{2} - mgl\cos 0 = \frac{1}{2}.m. 3lg - mgl.$$

$$v^{2} = 3lg - 2lg + 2lg. \frac{3}{5}$$

$$v^2 = 3lg - 2lg + 2lg$$

$$v^2 = \sqrt{\frac{11}{5}}$$

$$\sqrt{2} = \sqrt{\frac{11}{5}}$$

For P,

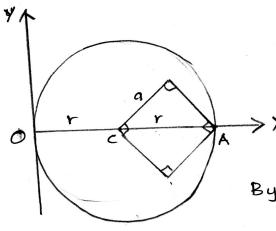
Applying F=ma

$$T - mg \cos \theta = \frac{mv^2}{l}.$$

$$T = \frac{11mlg}{5l} + \frac{3mg}{5}$$

$$T = \frac{14 \text{ mg}}{5}$$





$$2a^{2} = r^{2}$$

$$a = \frac{r}{\sqrt{2}}$$
Density - \(\rho \)

Density

By symmetry

Y=0:

Object	Mass	Distance from O to center. 9.	
	7 r2	F	(1
\$	190	3r 2	(4
Composite	(x-1) r2p	- 2 €	

$$(\pi - \frac{1}{2}) r^{2} g \overline{x} = \pi r^{2} g r - \frac{r^{2}}{2} \rho g \times \frac{3r}{2} (0)$$

$$(\frac{2\pi - 1}{2}) \overline{x} = (\frac{4\pi - 3}{4}) r.$$

$$\overline{x} = \frac{4\pi - 3}{2(2\pi - 1)} r. (5)$$

8) Of P.F=0

By the Law of Conservation of energy, $\frac{1}{2} \frac{2mg(x-l)^2}{l} - mgx = \frac{1}{2}m \cdot 2gl$ $\frac{1}{2} \frac{2mg(x-l)^2}{l} = l + x \cdot 5$

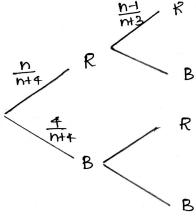
 $x^2 - 2xl + l^2 = l^2 + xl.$

x = 31. (x>0) travelled by the The maximum distance particle is 31.



9)
$$P(AUB) = P(A) + P(B) - P(ANB)$$
 (5)
 $\frac{9}{10} = \frac{2}{3} + \frac{1}{2} - P(ANB)$ (5)
 $P(ANB) = \frac{1}{3} + \frac{1}{2} - \frac{9}{10}$
 $P(ANB) = \frac{1}{15}$ (5)
 $P(A'NB) = P(B) - P(ANB)$ (5)
 $P(A'NB) = \frac{1}{2} - \frac{1}{15}$
 $= \frac{7}{30}$ (5)

10)



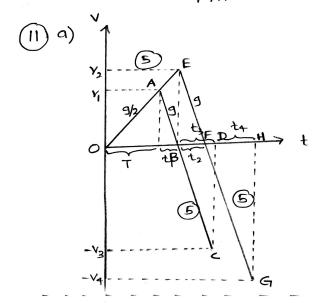
$$\left(\frac{n}{n+4}\right)\left(\frac{n-1}{n+3}\right) = \frac{1}{3} \qquad (D)$$

$$3n^2 - 3n = n^2 + 7n + 12$$

$$n^2 - 5n + b = 0 \qquad (5)$$

$$(n-b)(n+1) = 0$$

$$n=b \quad or \quad n=-1 \qquad (5)$$
but $n \neq -1$, ... $n=b \quad (5)$



$$\frac{AB}{T}, \frac{V_1}{t_1} = 9$$

$$V_1 = \frac{9T}{2}$$

$$t_1 = \frac{V_1}{9}$$

$$t_1 = \frac{9V_2}{9}$$

$$t_1 = \frac{T}{2}$$
(5)

Maximum height reached = Area of OAB by the released part = $\frac{1}{2} \left(T + \frac{T}{2} \right) V_1$ = $\frac{1}{2} \left(\frac{3T}{2} \right) \left(\frac{9T}{2} \right)$

$$=\frac{397^2}{8}$$

$$\frac{OE}{T+T/2} = \frac{9}{2} \qquad \frac{E-D}{4} = \frac{9}{4} = \frac{9}{4}$$

$$\frac{V_2}{42} = \frac{9}{2}$$

$$\frac{V_2}{3T/2} = \frac{9}{2}$$

$$V_2 = \frac{39T}{4} = \frac{3T}{4} = \frac{3T}{4}$$

The maximum beigh reached = Area of OED
$$\stackrel{\bigcirc}{5}$$
by the shuttle
$$= \frac{1}{2} \left(T + \frac{1}{2} + \frac{37}{4} \right) \stackrel{\cancel{391}}{\cancel{4}}$$

$$= \frac{1}{2} \left(\frac{97}{4} \right) \left(\frac{397}{4} \right)$$

$$= \frac{2797}{32} \stackrel{\bigcirc}{5}$$

20

Maximum height reached = Distance travelled by released part to reach the earth

Area of DAB = Area of BCD

$$\frac{397^2}{8} = \frac{1}{2} t_3 v_3$$

$$\frac{BC}{t_3} = 9$$

$$\frac{V_3}{t_3} = V_3$$

$$\frac{v_3}{q} = V_3$$

By (1),
$$\frac{39T^2}{8} = \frac{1}{2} \frac{\sqrt{3}}{9} \cdot \sqrt{3}$$

 $V_3 = \frac{39^2T^2}{4}$
 $V_3 = \frac{139T}{2}$ [10].

Maximum height reached = Distance travelled by shuttle to reach earth.

Area of OEF = Area of FAH

$$\frac{2797^{2}}{32} = \frac{1}{2} t_{4} v_{4} = \frac{3}{5},$$

$$\frac{2797^{2}}{32} = \frac{1}{2} t_{4} v_{4} = \frac{3}{5},$$

$$\frac{2797^{2}}{4} = \frac{1}{2} \cdot \frac{v_{4}}{9} \cdot v_{4}$$

$$\frac{2797^{2}}{32} = \frac{1}{2} \cdot \frac{v_{4}}{9} \cdot v_{4}$$

$$\frac{2797^{2}}{32} = \frac{1}{2} \cdot \frac{v_{4}}{9} \cdot v_{4}$$

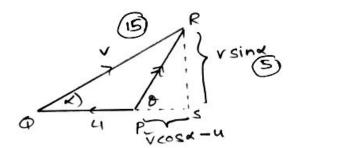
$$\frac{2797^{2}}{32} = \frac{1}{2} \cdot \frac{v_{4}}{9} \cdot v_{4}$$

$$\frac{3}{32} = \frac{1}{2} \cdot \frac{v_{4}}{9} \cdot v_{4}$$

$$\frac{3}{32} = \frac{1}{2} \cdot \frac{v_{4}}{9} \cdot v_{4}$$

11) b)
$$V_{D,E} \rightarrow U$$

$$V_{S,E} \stackrel{\nearrow}{\nearrow} V$$



D d tocus of s relative to D.

Shortest distance $DE = a \sin(90-0)$ = $a \cos \theta$. (5)

PRS
$$\Delta$$

$$\cos \theta = \frac{v \cos \alpha - u}{(v \cos \alpha - u)^2 + (v \sin \alpha)^2} = \frac{a (v \cos \alpha - u)^2 + (v \sin \alpha)^2}{\sqrt{v^2 + u^2 - 2uv \cos \alpha}}$$

Time taken for shortest? = $\frac{SE}{PR} = \frac{a \sin 6}{PR} (5)$ distance = $\frac{a v \sin \alpha}{(v \cos \kappa - u)^2 + (v \sin \kappa)^2} (10)$ $\frac{(v \cos \kappa - u)^2 + (v \sin \kappa)^2}{(v \cos \kappa - u)^2 + (v \sin \kappa)^2}$

$$11 - \frac{\sqrt{\sqrt{2} + \sqrt{2} - 2} \sqrt{\cos x}}{\sqrt{\sqrt{2} + \sqrt{2} - 2} \sqrt{\cos x}}$$

(30)

12) b) For
$$m, \leftarrow F = ma$$

$$T = m(f - F) - D(0)$$
For $2m, \downarrow F = ma$

For system, \rightarrow F = ma

1) +2

$$2mg = 3mf - mF$$

 $2g = 3f - F - 4$
 $f = \frac{2g+F}{3}$ 5

$$A_{M,E} \rightarrow F$$
 $A_{m,M} \neq A_{m,E}$
 $A_{2m,M} \downarrow f$
 $A_{m,E} = f + F$

$$a_{n,t} = f + \frac{1}{2}$$

$$a_{2m,t} = 4f + \frac{1}{2}$$

$$a_{2m,t} = 4f + \frac{1}{2}$$

25

From 3

$$0 = (M+3m)F - m(\frac{2g+F}{3}, \frac{6}{3})$$

$$O = \left(M + 3m - \frac{m}{3}\right) F - \frac{2mq}{3}$$

$$\frac{2mq}{3} = \left(\frac{3M+8m}{3}\right)F$$

$$F = \left(\frac{2mq}{3M + 8m}\right) (5)$$

$$from (3), f = \frac{1}{m} (M+3m) (\frac{2mq}{3M+8m})$$

$$a = \sqrt{\frac{2mq}{3M+8m}^2 + \left(\frac{2(M+3m)q}{3M+8m}\right)^2} = \sqrt{\frac{2mq}{3M+8m}}$$

Applying the Principle of Conservation of energy.

Applying lox F=ma for P,

$$R+T-mg\cos\theta=\frac{mv^2}{\alpha}$$
 (10)

$$R = -T + mg\cos\theta + \frac{m}{a} ga(k-2+2\cos\theta)$$

For the equlibrium of Q.

$$T-Mg=0$$

$$T=Mg = 5$$

$$R = -Mg + mg\cos\theta + \frac{m}{a} \cdot ga(\kappa-2 + 2\cos\theta)$$

When k=b.

$$R = mg \left[b - 2 + 3\cos\theta - \frac{M}{m} \right] \left(\frac{5}{3} \right)$$

$$= mg \left[4 + 3\cos\theta - \frac{M}{m} \right]$$

45

When the reaction disappeared.

then the
$$R = 0$$
 (5)

$$mg(4+3\cos\theta-\frac{M}{m})=0$$

$$\cos \theta = \frac{M - 4}{m} \boxed{5}$$

$$1 > \frac{M}{m} - 4 > -1$$
 5

$$3 > \frac{M}{m} - 4 > -3$$

$$7 > \frac{M}{m} > 1$$

The reaction is disappeared when

13)
$$\begin{cases} \sqrt{T} & 0 \\ \sqrt{T} & \sqrt{T} \\ \sqrt{P} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} \\ \sqrt{P} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} \\ \sqrt{P} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} \\ \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} & \sqrt{T} \\ \sqrt{T} & 0 \end{cases}$$

$$\begin{cases} \sqrt{T} & \sqrt{T} &$$

$$\int v^2 u^2 + 2as$$

$$\uparrow F=mq$$
 $T-mg=0$

$$\frac{\lambda \ell}{5} = mg = 0$$

$$\lambda = mg(5)$$

$$V^{2} = 0 + 29 \frac{10}{10}$$
 $V = \sqrt{291}$

$$mg-t'=mx$$

$$mg - mg\left(\frac{x-\ell}{\ell}\right) = m\dot{x}$$

$$-\frac{g}{\ell}(x-\ell-\ell) = \dot{x}$$

$$-\frac{9}{9}(x-\ell-\ell) = \frac{2}{3}$$

$$-\frac{9}{l} \left(x - 2l \right) = \cancel{x} \cancel{5}$$

.' The motion is simple harmonic.
$$\omega = 9$$

+ diagram 30

$$2e^{2} = \omega^{2}(A^{2}-x^{2}),$$

$$2e = \sqrt{2}e, \quad \omega = \sqrt{9}e, \quad x = l. \quad (10) \text{ conditions}$$

$$2gl = \frac{9}{l}(A^{2}-l^{2})$$

$$3e = \sqrt{3}A$$

$$2l^{2}+l^{2} = A^{2}$$

$$4 \text{ diagram } 30$$

$$2e = \sqrt{9}e, \quad x = l. \quad (10) \text{ conditions}$$

$$2gl = \frac{9}{l}(A^{2}-l^{2})$$

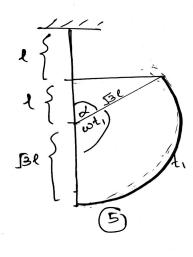
$$3e = \sqrt{3}A$$

$$2l^{2}+l^{2} = A^{2}$$

$$4^{2} = 3l^{2}$$

$$A^2 = 3\ell^2$$

To calculate the time, let consider a horizontal circular motion of radius J32 moving with w angular relocity. (5)



$$\cos x = \frac{1}{5} (5)$$

$$x = \cos^{3}(75)(5)$$

$$wt_{1} = x - x \cdot (5)$$

$$= x - \cos^{3}(\frac{1}{5})$$

$$t_{1} = \frac{1}{5} (x - \cos^{3}(\frac{1}{5}))$$

$$= \frac{1}{9} (x - \cos^{3}(\frac{1}{5}))$$

For the motion from 0 to distance 1, 30

$$\int_{2g_1}^{2g_1} = 0 + g + 2 = 5$$

$$+ 2 = \sqrt{\frac{21}{9}} = 5$$

10

Time taken by particle to reach the maximum distance from O,

$$t_1 + t_2 = \sqrt{\frac{2}{9}} \left\{ x - \cos \frac{1}{13} \right\} + \sqrt{\frac{27}{9}}$$

$$= \sqrt{\frac{1}{9}} \left\{ x - \cos \frac{1}{13} + 5^{2} \right\} (5)$$

Time taken to reach the maximum height is equal to the time taken by particle to return 0.

.: Total time taken to reach =
$$2\sqrt{\frac{1}{9}} \left\{ x - \cos \frac{1}{12} + \sqrt{\frac{1}{2}} \right\}$$
o again

[70]

$$\overrightarrow{OX} = \lambda \overrightarrow{OC}$$

$$\overrightarrow{OX} = \lambda (\overrightarrow{OA} + \overrightarrow{AC}) (5)$$

$$\overrightarrow{OX} = \overrightarrow{OB} + \cancel{BX} (5)$$

$$= \overrightarrow{OB} + \cancel{BX} (6)$$

$$= \overrightarrow{OB} + \cancel{A} (\cancel{BO} + \cancel{OD})$$

$$= \cancel{D} + \cancel{D} + \cancel{D} (\cancel{D} + \cancel{OD})$$

$$= \cancel{D} + \cancel{D} + \cancel{D} + \cancel{D} (\cancel{D} + \cancel{D} + \cancel{D$$

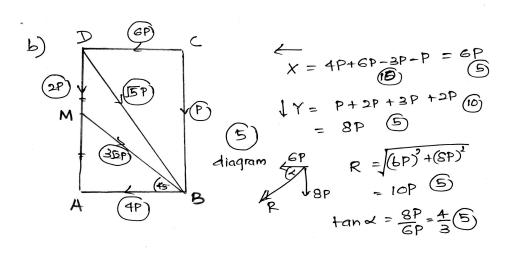
$$0 \times 1 \times 1 = 400$$

$$0 \times 1 \times 1 = 1135$$

$$0 \times 1 \times 1 = 311$$

$$0 \times 1 \times 1 = 311$$

$$0 \times 1 \times 1 = 311$$



$$A_{ij}G_{ij} = P.a - bP. 2a + 355P. \frac{a}{5} + 55P. \frac{a.2}{5}$$

$$= P.a - 12Pa + 3Pa + 2Pa. 6$$

$$= -bPa 6$$

There is a couple of moment 6Pa in anticlockwise 5

70

For the equ. of AI

$$X_1 \times 4a \cos 30 = 2W$$
 $X_1 \times 4a \cdot \frac{3}{2} = 2W$
 $X_1 = \frac{W}{2J_3}$
 $X_1 = \frac{W}{2J_3}$

For the equi. of CD.

To the
$$\frac{1}{2}$$
 $\frac{1}{2}$ $\frac{1}{2}$

Reaction at
$$C = \sqrt{\left(\frac{W}{2J_3}\right)^2 + W^2}$$

$$= \frac{W}{2J_3} \left(\frac{13}{3}\right) \left(\frac{5}{3}\right)$$

$$\tan \theta = \frac{W}{W/2J_3}$$

$$\theta = \tan^{1}(2J_3) \left(\frac{5}{3}\right)$$

ii) For the equ^m of BC.

B)
$$T \times \frac{3a}{3} \sin 30^{\circ} - w \cdot x a \sin 30^{\circ} - x_{1} \times 2a \cos 30$$

$$- y_{1} \times 2a \sin 30^{\circ} = 0 \quad 10$$

$$T \times \frac{3a}{3} \times \frac{1}{3} = w \cdot \frac{a}{3} + \frac{w}{2} \times 2a \times \frac{5a}{3} + w \times 2a \times \frac{1}{2}$$

$$\frac{3T}{4} = \frac{w}{3} + \frac{w}{3} + w$$

$$\frac{3T}{4} = 2W$$

$$T = \frac{8W}{3}$$
(5)

iii). For the equ^m of BC,

$$x_2 = x_1 = \frac{w}{2J_3}.$$

$$4_2 = -T + y_1 + w.$$

$$y_2 = -\frac{8w}{3} + 2w.$$

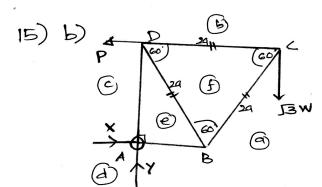
$$y_3 = -\frac{2w}{3}.$$

Reaction at B =
$$\left(\frac{W}{2J_3}\right)^2 + \left(\frac{2W}{3}\right)^2$$

= $\frac{\sqrt{19}}{6}$ w (5)

$$tan d = \frac{2W/3}{W/2J3}$$

$$d = tan' (\frac{4}{J3})$$



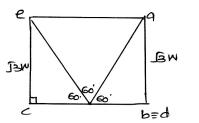
For the eq of system,

$$\rightarrow x = P = 2W$$

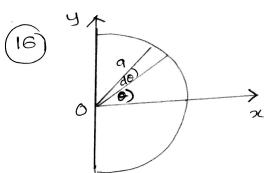
$$\uparrow \quad \gamma = J_3 w.$$
Reaction at $A = \sqrt{(2w)^2 + (J_3 w)^2}$ 5

$$tan \theta = \frac{13}{2}$$

$$6 = \tan^{1} \frac{\sqrt{3}}{2}$$



tod	Magnitude	Tension/Thrust
AB (ea)	2W	Thrust
AD(ce)	13 W	Thrust
BD(ef)	2₩	Tension
BC(af)	2W	Thrust
CD (bf)	W	Thrust
	(25)	(25)



symmetry, the center of mass lies on on axis. 5

is the mass per unit area.

$$x = \frac{29}{3}\cos\theta$$

$$dm = 1.9^2 d\theta$$

$$dm = \frac{1}{2}a^2 d\theta P$$
.

$$\frac{\pi}{2} = \int_{\frac{\pi}{3}}^{\frac{\pi}{2}} \frac{2a \cos \alpha \times \frac{1}{2}a^{2} d\alpha\beta}{\frac{\pi}{2}a^{2} d\alpha\beta} \cdot \frac{5}{5}$$

$$\frac{\pi}{2} = \int_{\frac{\pi}{3}}^{\frac{\pi}{2}} \frac{2a \cos \alpha \times \frac{1}{2}a^{2} d\alpha\beta}{\frac{\pi}{2}a^{2} d\alpha\beta} \cdot \frac{5}{5}$$

$$\frac{\pi}{2} = \frac{2a}{3} - \frac{\pi}{3} \frac{\pi}{2} \cos \alpha d\alpha$$

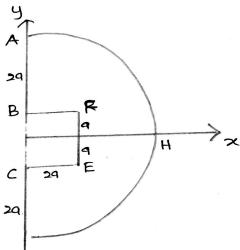
$$= \frac{2a}{3} - \frac{\pi}{3} \frac{\sin \alpha}{3} - \frac{\pi}{3} \frac{5}{3}$$

$$= \frac{2a}{3} \left[\frac{\sin \alpha}{3} - \frac{\pi}{3} \right] \cdot \frac{5}{3}$$

$$= \frac{2a}{3} \left[\frac{\sin \alpha}{3} - \frac{\pi}{3} \right] \cdot \frac{5}{3}$$

$$= \frac{29}{3} \times \frac{2}{\pi}$$

$$=\frac{49}{3\pi} (5)$$



By symmetry, the center of mass lies on the Ox axis. (5)

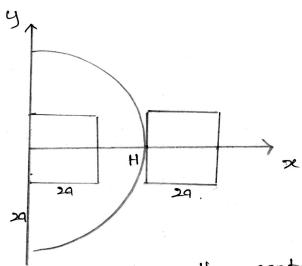
p is the mass per unit area.

				THE RESERVE THE PROPERTY OF THE PERSON NAMED IN COLUMN TWO IS NOT THE PERSON NAMED IN COLUMN TWO IS NAMED IN COLUMN TWO I	-
-	object	Mass	- F 1-3	Distar	O
		7 (3a)2 = 0	2 (5)	4(39) =	49 7. (5)
West of the subsection of the second subsection of the second		4ap	(E)	9	(5)
Section to the section of the sectio	D	(97-8)	a ² / (3)	त्र	

$$\left(\frac{9\pi-8}{2}\right)a^{2}\rho = \frac{9\pi a^{2}\rho}{2} \times \frac{49}{\pi} - 4a^{2}\rho \times 9$$

$$\left(\frac{9\pi-8}{2}\right)\pi = (18-4)9$$

$$\pi = \frac{289}{9\pi-8} = 5$$



By Symmetry, the center of mass lies on

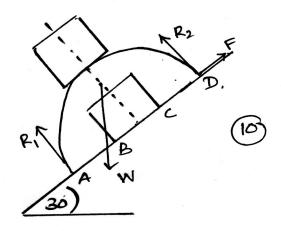
X 3111-1					
	Object	mass	Distance from 0		
	5	(<u>9x-8</u>) 033	289 97-8	(5)	
		40 ² p.	49	(5)	
	20	9×92 p. (5)	7		

$$\frac{9\pi a^{2}}{2} \rho \overline{\chi} = \left(\frac{9\pi - 8}{2}\right) a^{2} \rho \left(\frac{289}{9\pi - 8}\right) + 4a^{2} \rho . \pi 49$$

$$\frac{9\pi}{2} \overline{\chi} = 1149 + 1169. \quad \boxed{5}$$

$$\overline{\chi} = \frac{60}{9\pi} 9$$

$$\overline{\chi} = \frac{20}{3\pi} 9 \quad \boxed{5}$$



$$R_1 + R_2 = w \cos 30^{\circ} (5)$$

For the equilibrium,

$$\mu \geqslant \left| \frac{F}{R_1 + R_2} \right|$$
 (10)

$$\mu > \frac{w \sin 30}{w \cos 30}$$

17) a) i) If
$$A \cap B = \emptyset$$
, then A and B are mutually exclusive events. (5)
ii) If $A \cup B = \Omega$, then A and B are exhaustive. (5)

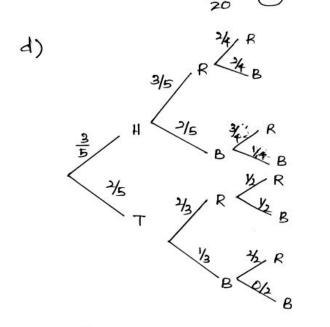
b) P(A) + P(B) + P(C) = P(A) (5) $2a^{2} + 2a + 8a - 1 = 1$ (5) $2a^{2} + 10a - 2 = 0$ $a^{2} + 5a - 1 = 0$ (5) $(a + \frac{5}{2})^{2} = \frac{1 + 25}{4}$ $a + \frac{5}{2} = \frac{1 + 29}{2}$ (7) $a = -\frac{5}{2} + \frac{129}{2}$ (5) As a > 0, $a = \frac{124 + 5}{2}$ (5)

c) i)
$$A = (A \cap B) \cup (A \cap B^{1})$$
 (5)
$$P(A) = P[(A \cap B) \cup (A \cap B^{1})]$$

$$P(A) = P(A \cap B) + P(A \cap B^{1})$$
 (5) (1)
$$(: (A \cap B) \cap (A \cap B^{1}) = \bar{\phi})$$
 (5)

ii)
$$AUB = (AUB^{\dagger})UB = 5$$
 $AS (ANB^{\dagger}) \cap B = 4$
 $P(AUB) = P(AUB^{\dagger}) + P(B) = 1$
 $P(AUB) = P(A) + P(B) - P(ANB) = 1$
 $P(A) = P(ANB) + P(ANB^{\dagger})$
 $P(ANB) = \frac{3}{4} - \frac{2}{5} = \frac{7}{20} = \frac{5}{20}$
 $P(AUB) = P(A) + P(B) - P(ANB)$
 $P(AUB) = P(B) - P(ANB)$
 $P(A^{\dagger} \cap B) = P(B) - P(ANB)$

$$P(A'UB) = P(A') + P(B) - P(A' \cap B)$$
 (5)
= $\frac{1}{4} + \frac{1}{2} - \frac{3}{20}$ (5)
= $\frac{3}{5}$ (5)



i)
$$\frac{3}{5} \times \frac{3}{5} \times \frac{2}{4} + \frac{2}{5} \times \frac{3}{5} \times \frac{1}{2}$$
 (b)
= $\frac{18}{100} + \frac{2}{15}$



විභාග ඉලක්ක පහසුවෙන් ජයගන්න

පසුගිය විභාග පුශ්න පතු



 Past Papers
 Model Papers
 Resource Books for G.C.E O/L and A/L Exams





ົ້ວສາທ ໑ලສ່ສ ປ໌ຜທສ່ສ Knowledge Bank



WWW.LOL.LK







Website WWW.IOI.IK



071 777 4440